

All ELTs are planning to use multiple-LGS for Wide Field AO



Because lasers are cool – and make nice PR movies...

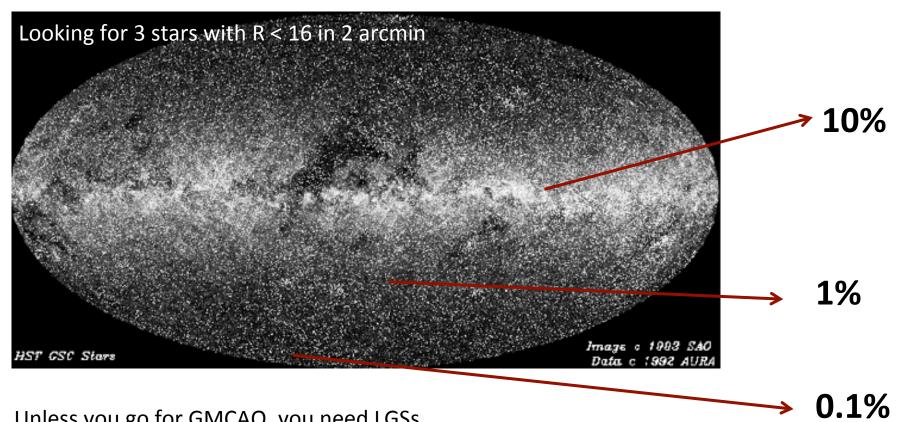






Lasers are required to get the sky coverage

How many Natural Guide Stars are available?



Unless you go for GMCAO, you need LGSs...

However... Lasers suffer from some fundamental limitations

Natural Guide Star are required to complement LGS measurements...



This will drive the sky coverage of LGS-assisted AO systems

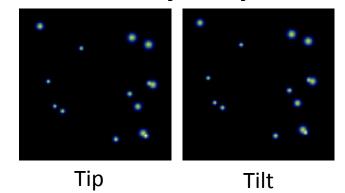
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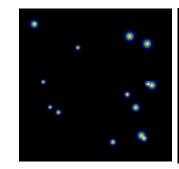
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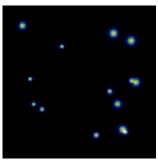
This will drive the sky coverage of LGS-assisted AO systems

Fortunately, only few modes need to measure:

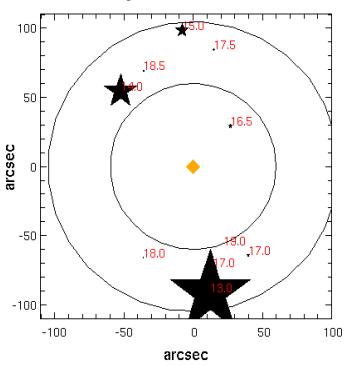








Question: how to estimate the sky coverage (or residual error on low order modes) for LGS assisted instruments?



It depends on many parameters...

the number of NGS we use, their magnitude, their configuration, the WFS characteristics (noise, spatial and temporal sampling) and of course, on the environment (seeing, LO, telescope windshake, ...)

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It depends on many parameters... let's try to simplify it...



Simulation strategy:

Residual errors are computed in an "error budget" fashion:

- <u>Tomography</u>: depends on the distance (and number) of the NGSs + Cn2
 - <u>Temporal errors</u>: this only depends on the NGS loop frequency.
- Noise propagation: This depends both on the distance and magnitude of the stars,
 as well as the WFS choice...

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Tomography

Temporal

Noise



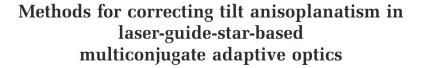
Compensation of the Null modes with the Gemini MCAO

Gemini Document RTP-AO-G0097

Francois Rigaut. February 29, 2000

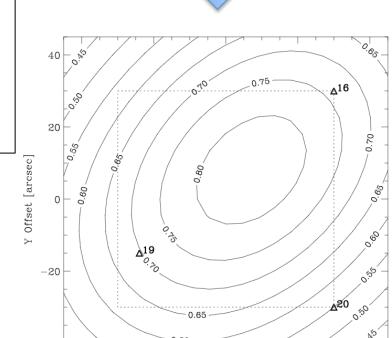
B. L. Ellerbroek and F. Rigaut

Vol. 18, No. 10/October 2001/J. Opt. Soc. Am. A 2539



Brent L. Ellerbroek and François Rigaut

Gemini Observatory, 670 North A'ohoku Place, Hilo, Hawaii 96720

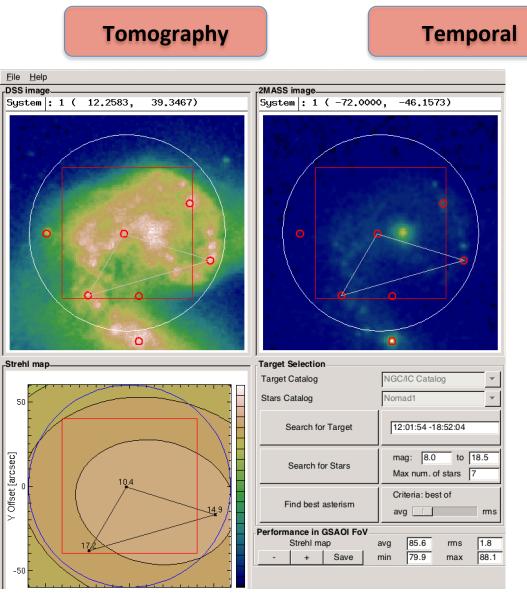


X Offset [arcsec]

20

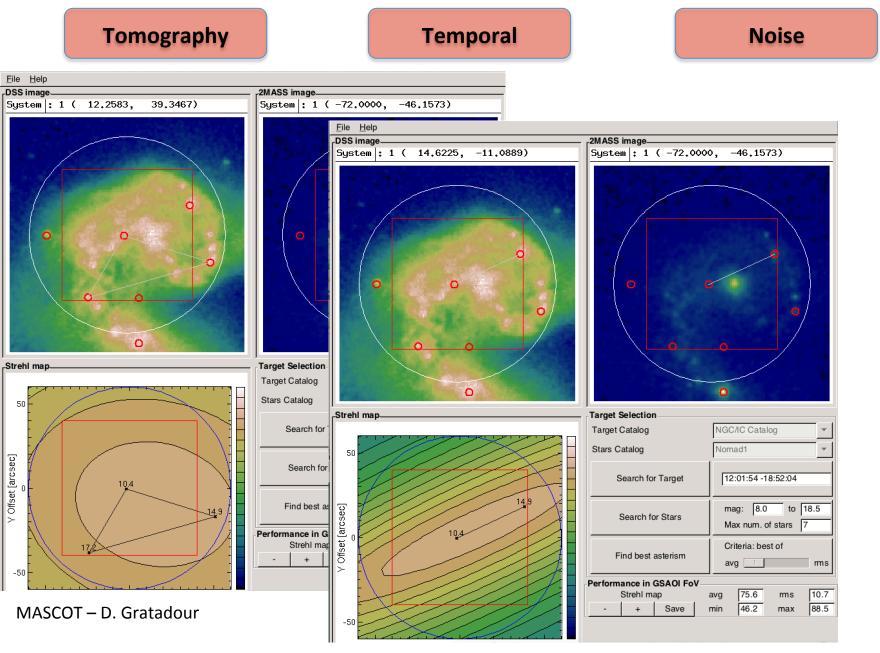
40

-40



MASCOT - D. Gratadour

Noise

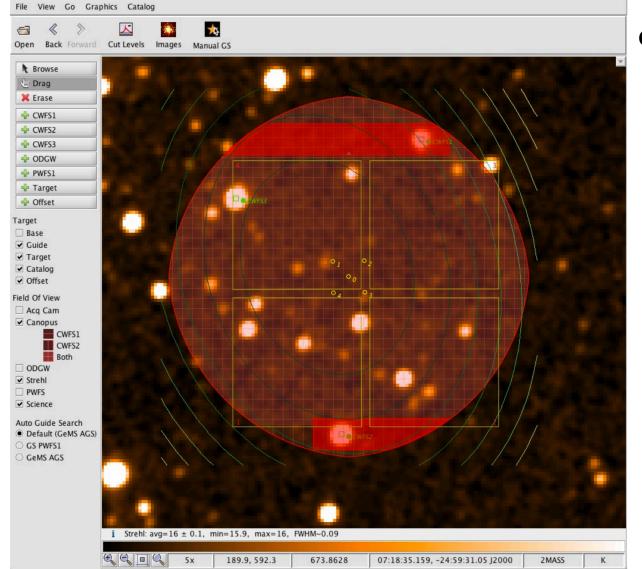


Tomography

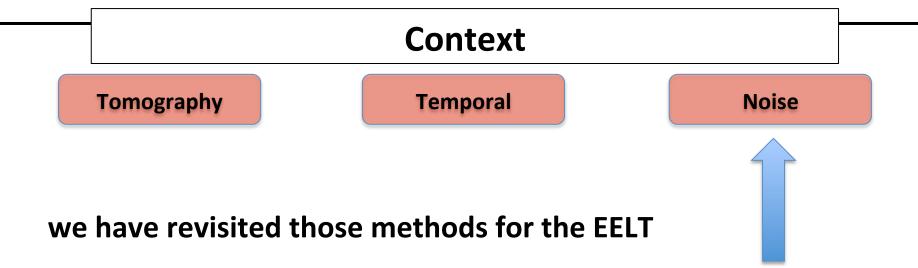
Temporal

Noise

Gemini Observing tool



Tomography Temporal Noise Go Graphics Catalog **Gemini Observing tool** Open Back Forward Cut Levels Images Manual GS **Browse Drag X** Erase Schrimer et al., ApJS, 2014 Cut Levels Images Manual GS -24°04 R Browse 117 X Erase ← CWFS2 81 ◆ ODGW PWFS1 💠 Target - Offset ☐ Base Dec (J2000) ✓ Guide ✓ Target ✓ Offset Field Of View 05 Acq Cam CWFS1 CWFS2 ODGW ✓ Strehl PWFS ✓ Science Auto Guide Search Default (GeMS AGS) GS PWFS1 GeMS AGS 10s 08s 06s 4h16m04s i Strehl: avg=6.9 ± 17.8, min=2.4, max=15.5, FWHM~0.09 RA (J2000) 3789.0 04:16:08.477, -24:04:49.16 J2000 439.5, 448.5

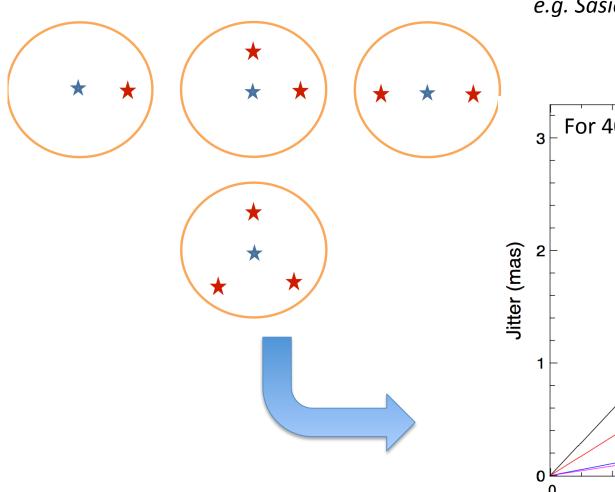


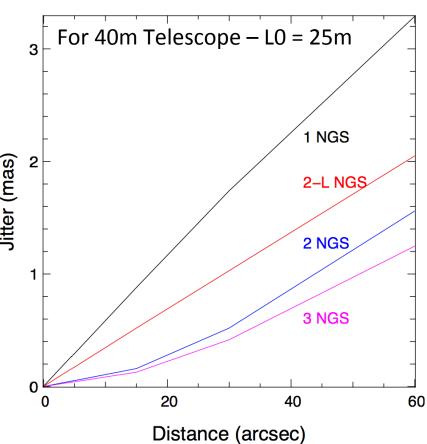
We have mainly worked on this term (but we'll review the 3 terms in the following slides)

Tomography

Impact on residual jitter of different NGS constellation

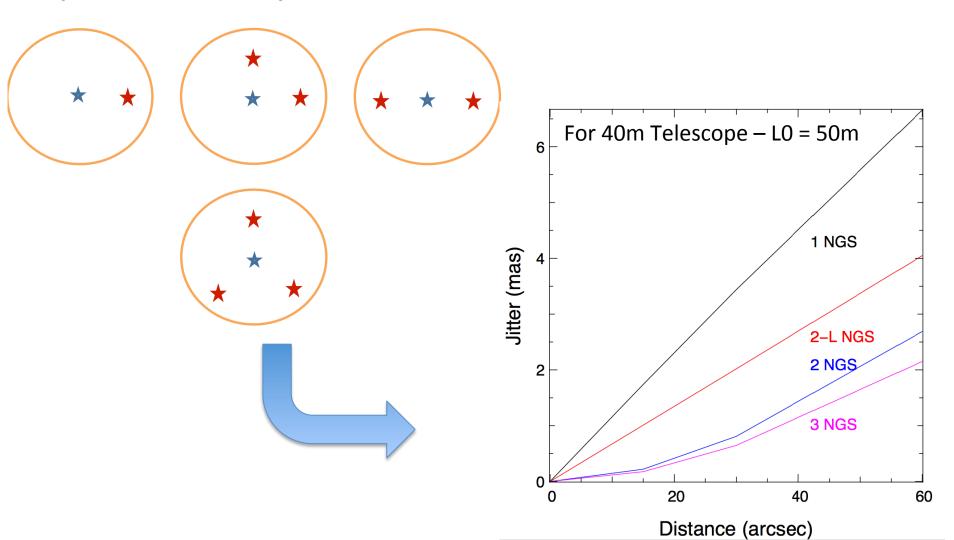
e.g. Sasiela, Chassat, Whiteley...





Tomography

Impact on residual jitter of different NGS constellation

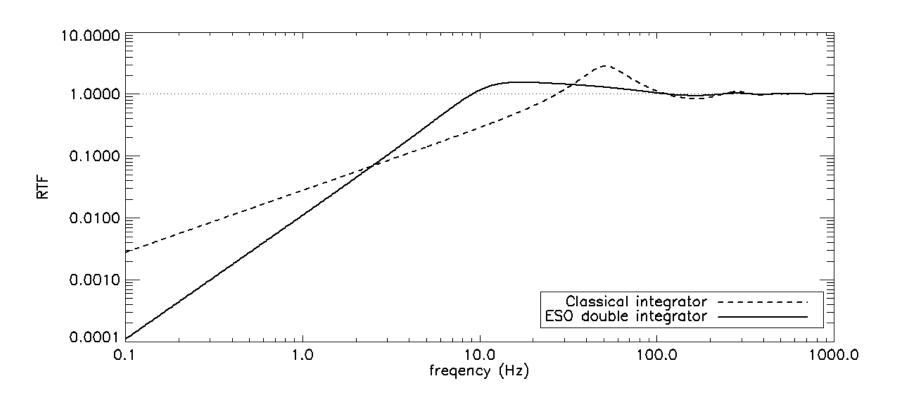


Temporal

First need to determine the rejection transfer function.

It depends on the controller performance...

Assuming ELT scheme with M4/M5 we could have:

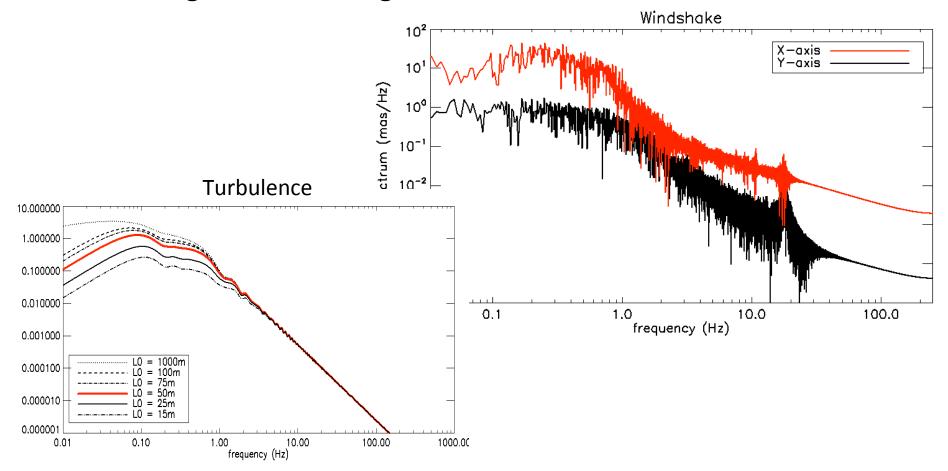


Temporal

First need to determine the rejection transfer function.

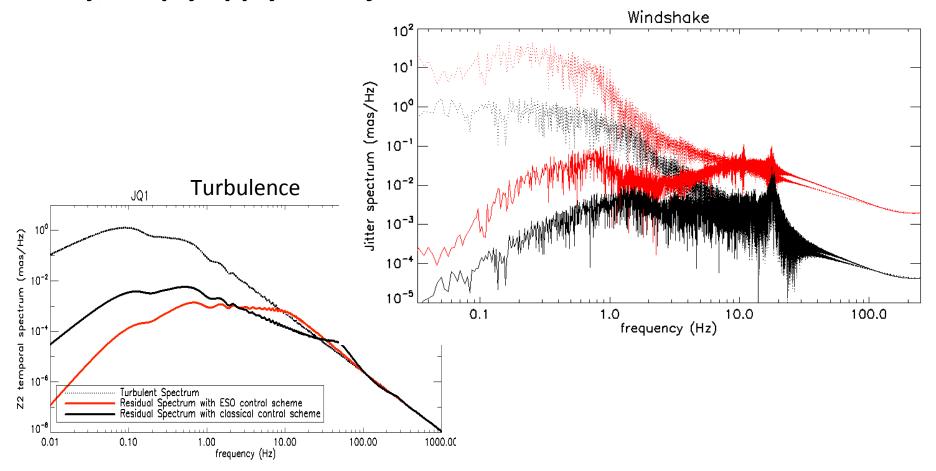
Then, need to know the inputs, it may be Turbulence and Windshake

Still assuming an EELT configuration, we have:



Temporal

First need to determine the rejection transfer function. Then, need to know the inputs, it may be Turbulence and Windshake Finally, simply apply the rejection:

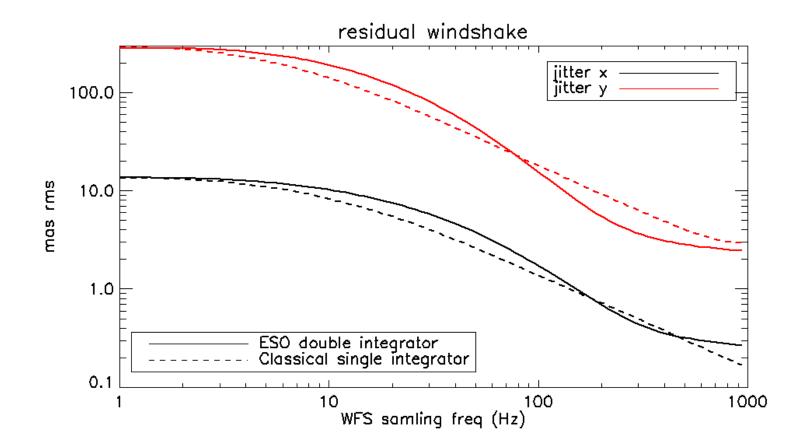


Temporal

First need to determine the rejection transfer function.

Then, need to know the inputs, it may be Turbulence and Windshake Finally, simply apply the rejection.

Eventually – play with the NGS gain, and loop frequency



Noise

Noise depends first of all on the WFS strategy chosen.

For instance, for SH, noise coefficients have been well studied, and are defined as: e.g. Rousset et al., Nicolle et al.

Photon Noise

$$\sigma_{ph,sspup}^2 = \frac{1}{2\ln(2)} \frac{1}{n} \left(\frac{N_T^2}{N_D^2} \right) \left(\frac{(N_T^2 + N_W^2)}{(2N_T^2 + N_W^2)} \right)^2$$

Read-Out Noise

$$\sigma_{ron,sspup}^2 = \frac{\pi}{32\ln(2)} \left(\frac{ron}{n}\right)^2 \left(\frac{\left(N_T^2 + N_W^2\right)}{N_D}\right)^2$$

Noise

FWM of subap. PSF

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Read-Out Noise

 $\sigma_{ron,sspup}^2 = \frac{\pi}{32\ln(2)} \left(\frac{ron}{n}\right)^2 \left(\frac{N_T^2 + N_W^2}{N_D}\right)^2$

$$\sigma_{total}^{2} = \frac{\left(\sigma_{ph,sspup}^{2} + \sigma_{ron,sspup}^{2}\right)}{N_{sspup,valid}}$$

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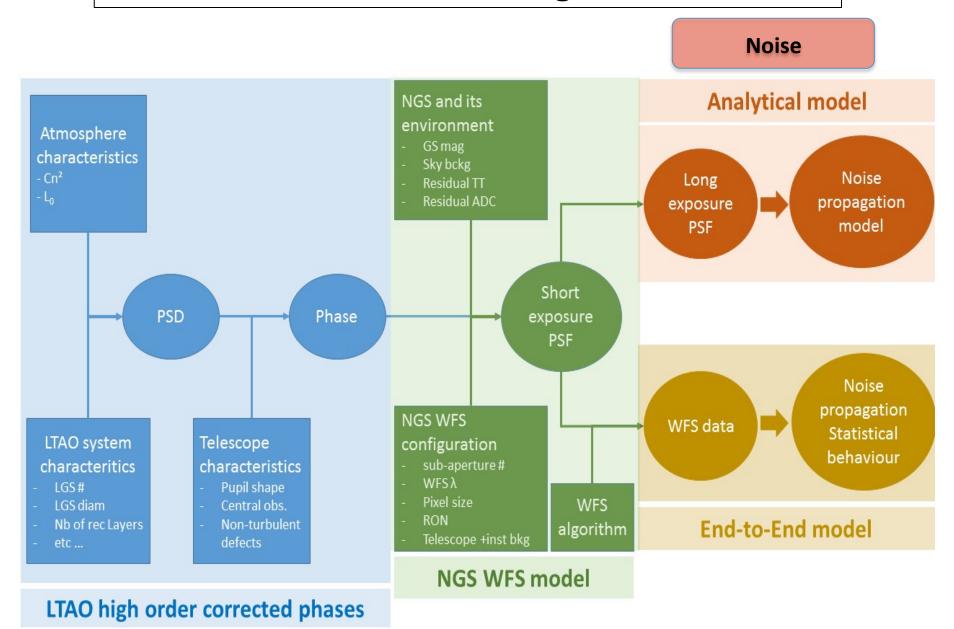
$$\sigma_{ph,sspup}^2 = \frac{1}{2\ln(2)} \frac{1}{n} \binom{N_T^2}{N_D^2} \left(\frac{\binom{N_T^2 + N_W^2}{(2N_T^2 + N_W^2)}}{\binom{2N_T^2 + N_W^2}{(2N_T^2 + N_W^2)}} \right)^2 \text{ weighting}$$

Read-Out Noise

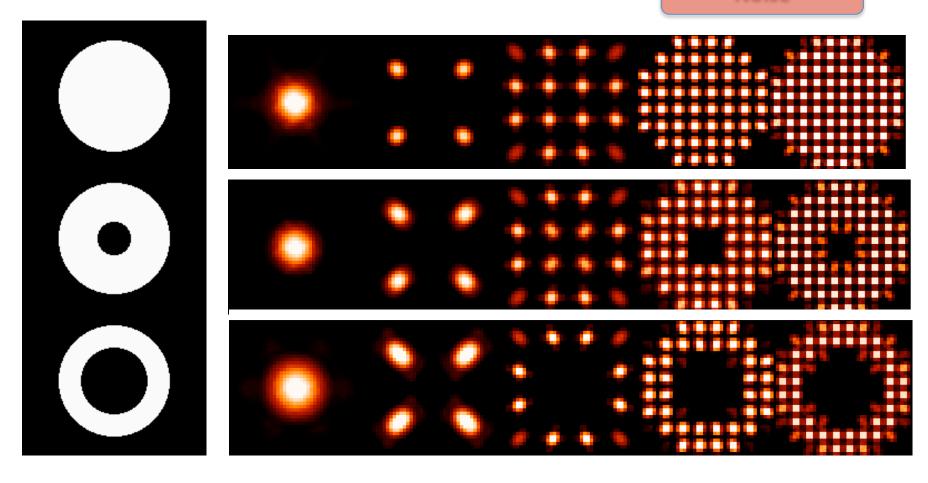
$$\sigma_{ron,sspup}^2 = \frac{\pi}{32\ln(2)} \left(\frac{ron}{n}\right)^2 \left(\frac{N_T^2 + N_W^2}{N_D}\right)^2$$

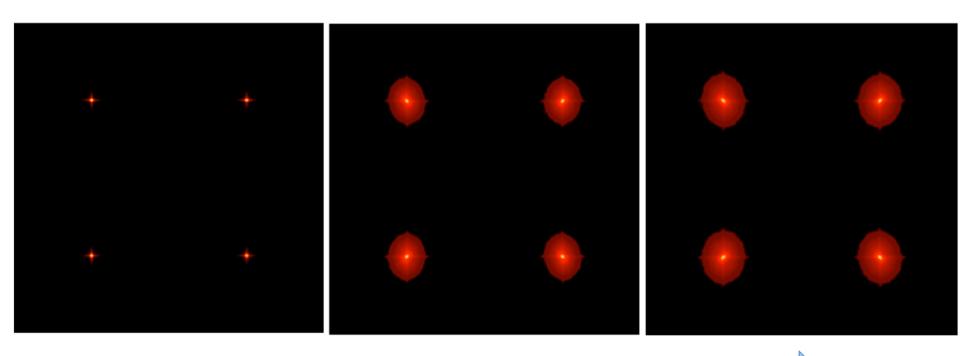
$$\sigma_{total}^{2} = \frac{\left(\sigma_{ph,sspup}^{2} + \sigma_{ron,sspup}^{2}\right)}{N_{sspup,valid}}$$

This is however not valid anymore in presence of residual turbulence.



Noise



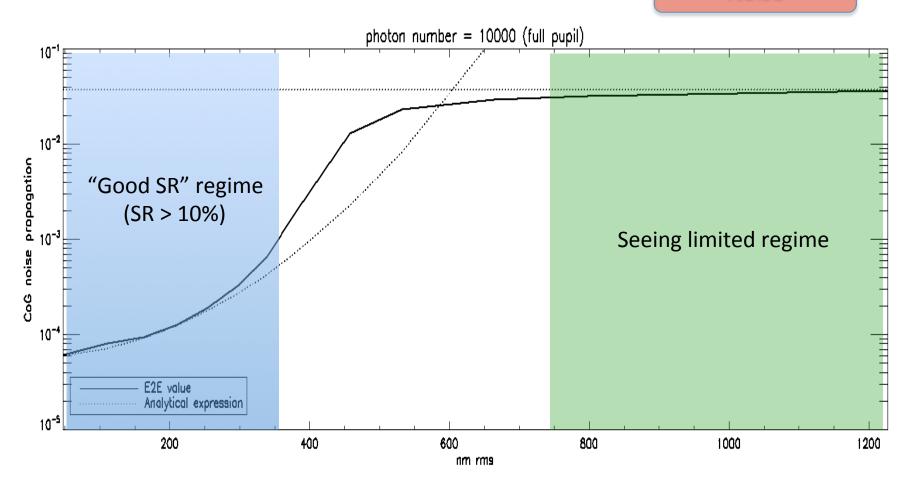


Increasing residual phase seen by the WFS

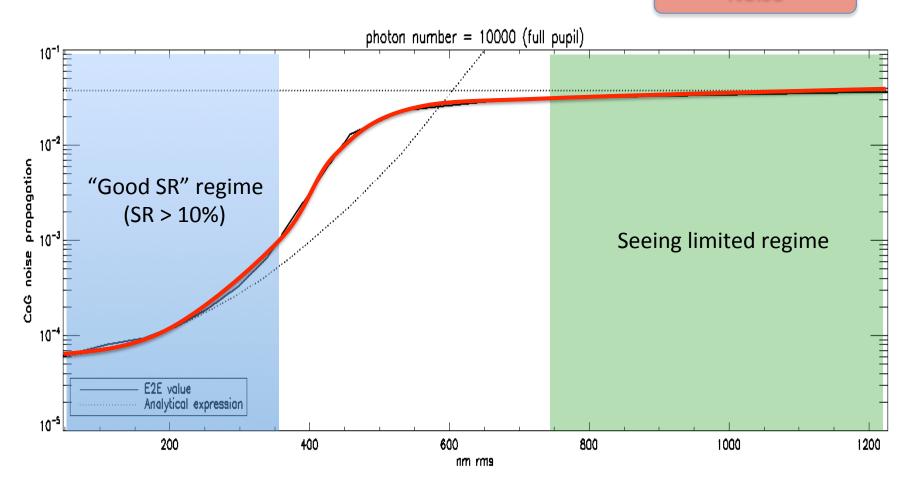
Good SR regimes

Seeing limited regimes





Noise



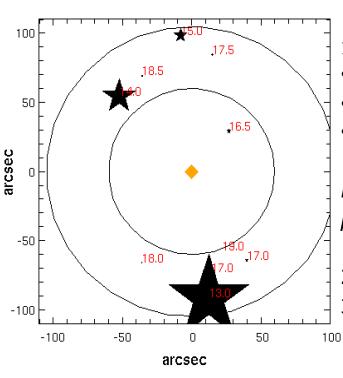
$$\sigma_{tot,all\;mas}^2 = \left(\frac{N_T}{N_D}\right)^2 \sigma_{tot,SR\;mas}^2 + \left(1 - \left(\frac{N_T}{N_D}\right)^2\right) \sigma_{tot,FWHM\;mas}^2$$

Tomography

Temporal

Noise

Question: how to estimate the sky coverage (or residual error on low order modes) for LGS assisted instruments?

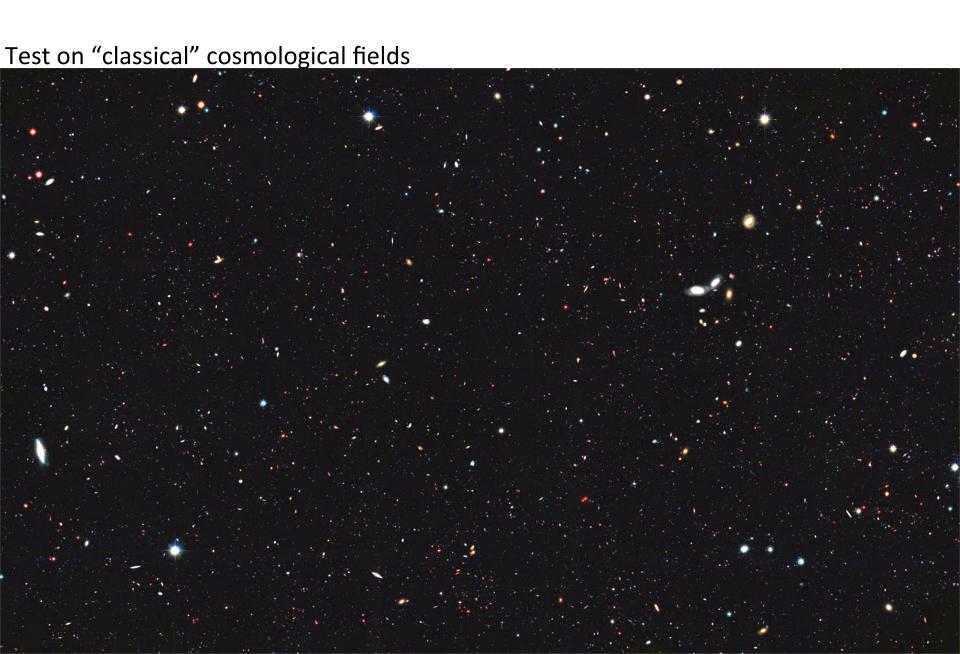


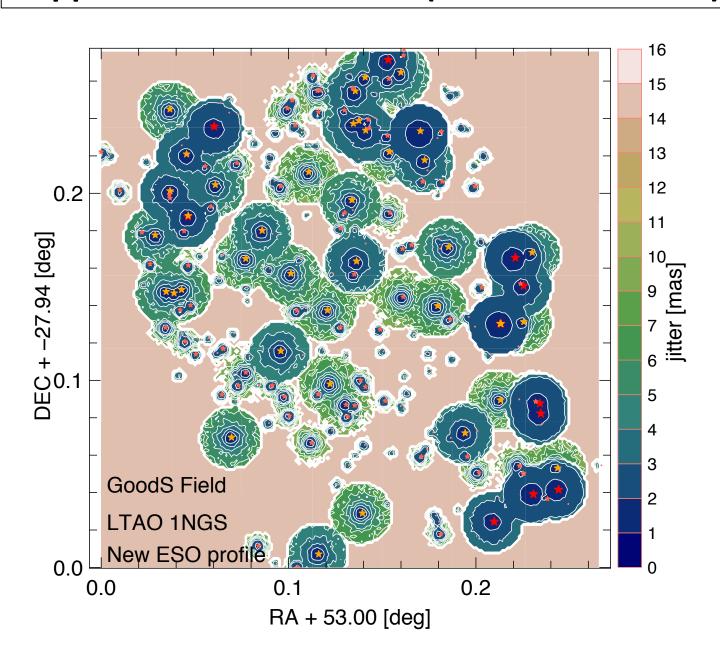
- 1. For a given field, we can compute, for each star:
- The anisoplanatism
- The temporal error
- The noise coefficient

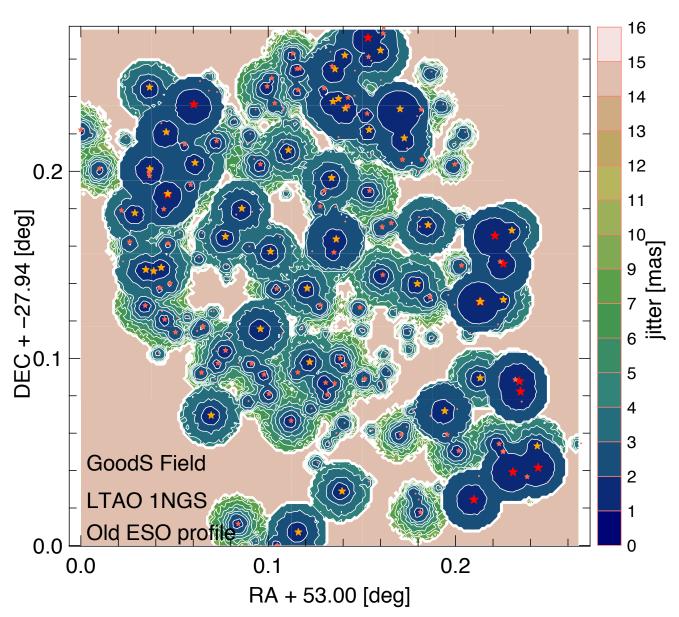
Note: an optimization between noise and temporal error can be performed

- 2. Reproduce the process for each pair of stars
- 3. Reproduce the process for each 3NGS constellation available

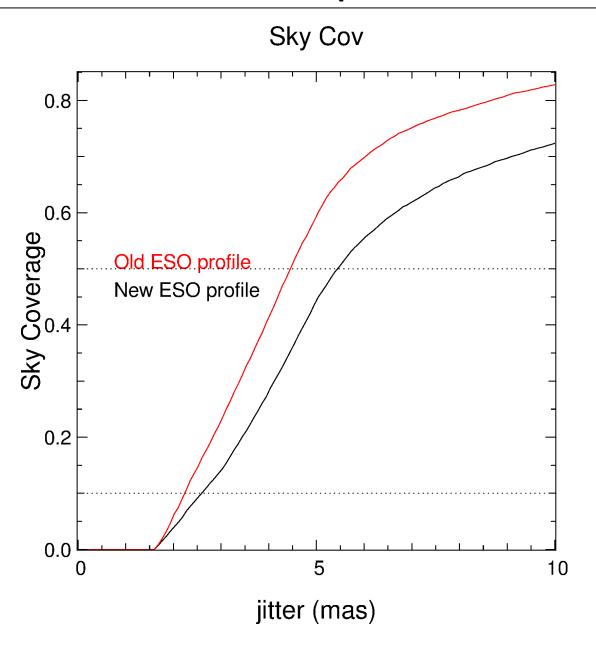
- This can be done on synthetic fields, generated from star distribution statistics
- This can de bone on real fields

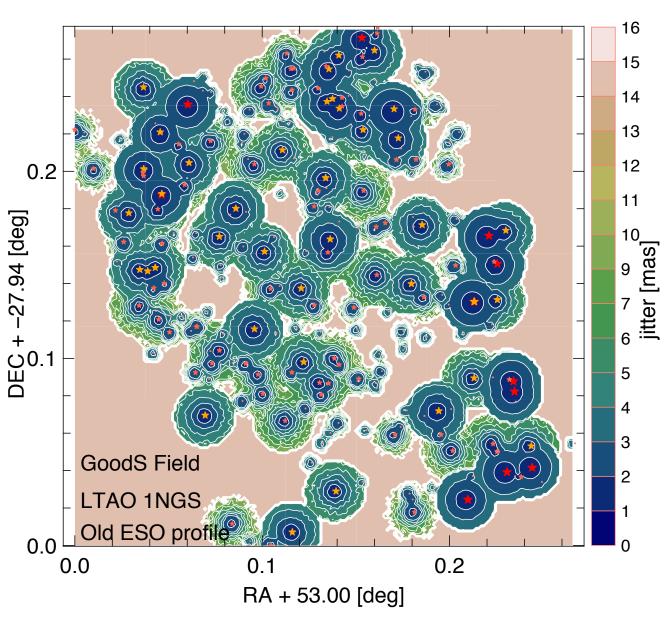




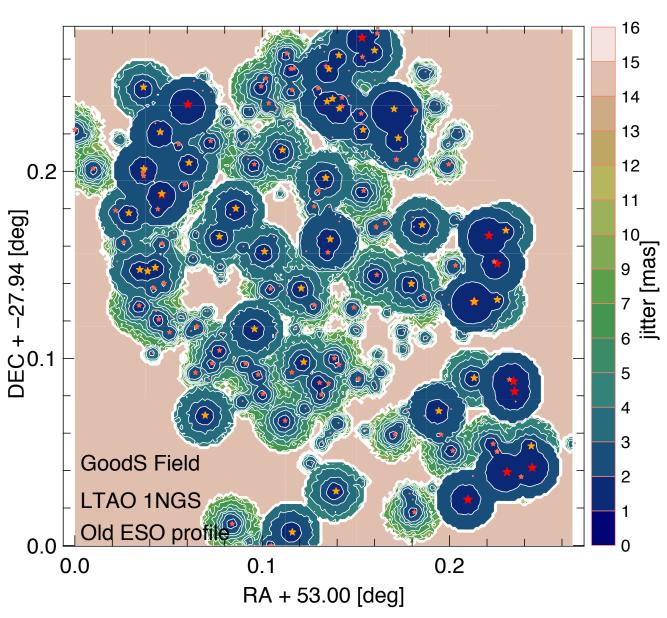


Impact of Cn2 profile (from old ESO to new 35 layers)

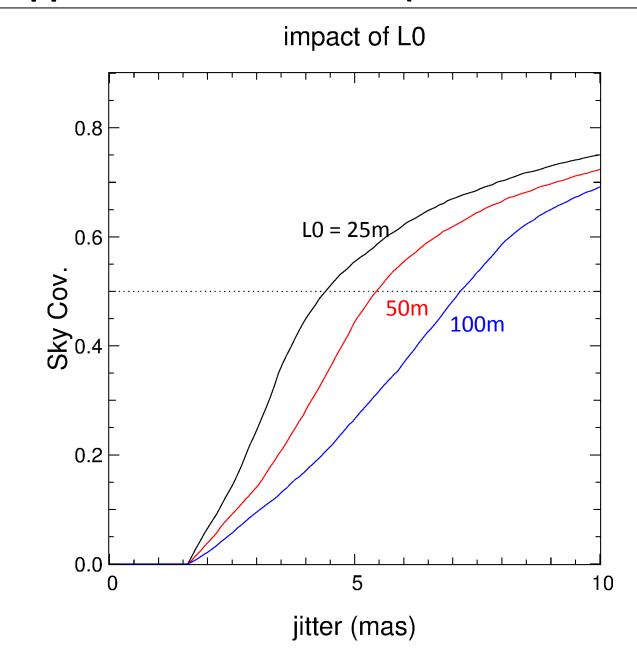




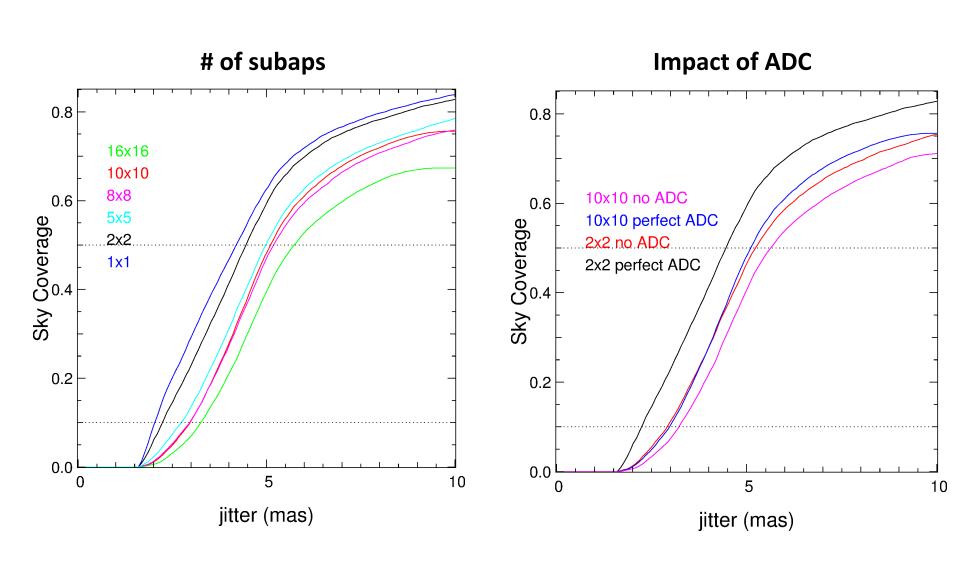
Impact L0 (from 50m to 25m)



Impact L0 (from 50m to 25m)

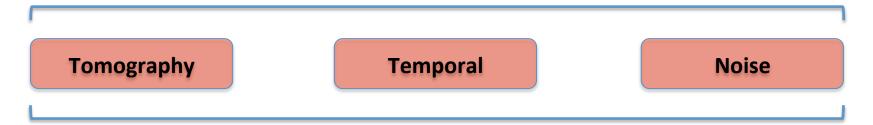


System trade-off



CONCLUSIONS

How to estimate the sky coverage (or residual error on low order modes) for LGS assisted instruments?



We have improved the noise model to account for residual turbulence, and other effects like ADC, pupils, etc...

So far we have considered full decoupling of NGS vs. LGS, but algorithms to take advantage of the higher-order (measured by the LGS) to improve further the could be envisioned (e.g. Gilles, Correia et al. (sort of PSF reconstruction in the NGS path)).