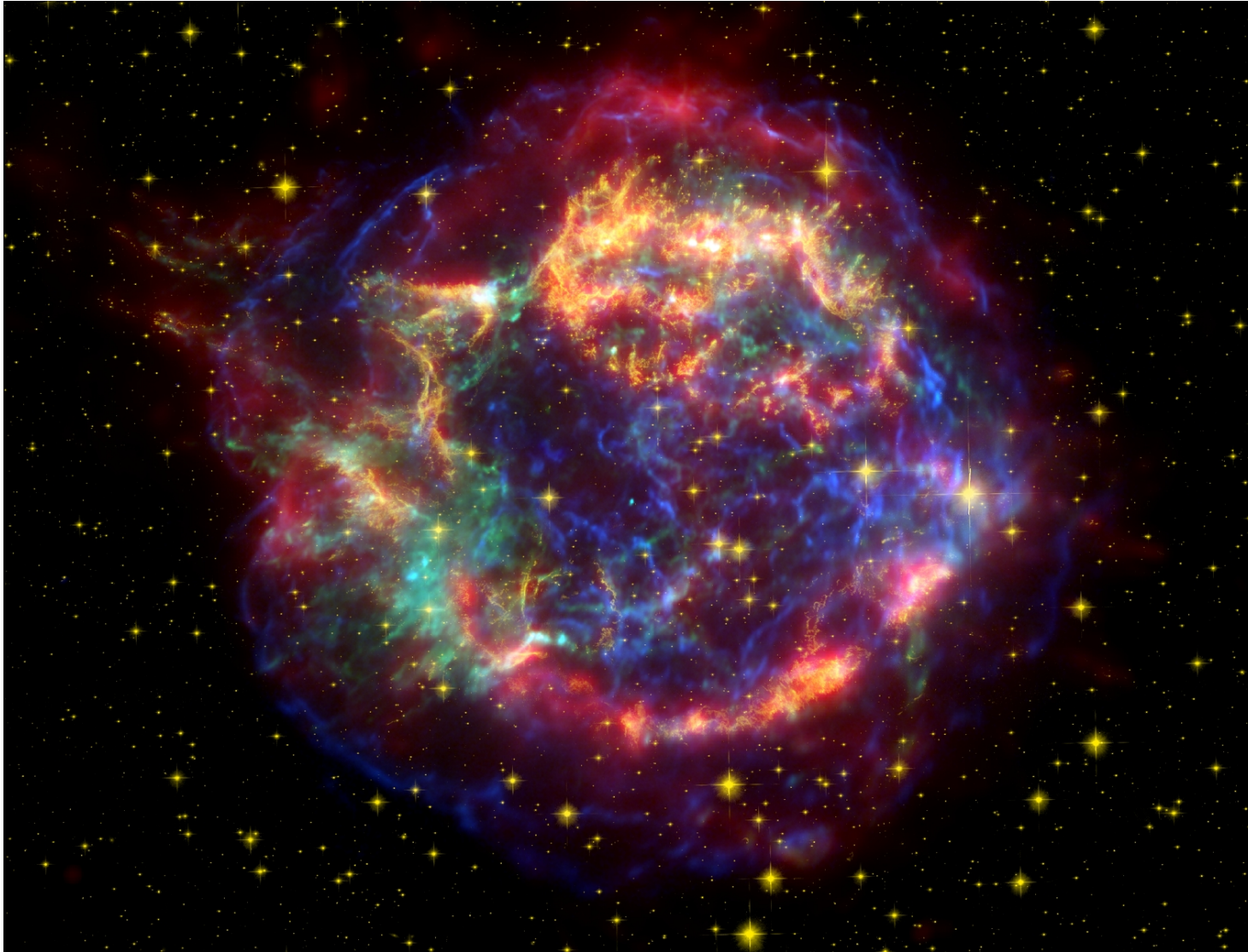


Supernova or direct collapse?

Supernova explosions and black hole mass

Core-collapse supernovae



When Fe core forms in a massive ($> 8 M_{\text{sun}}$) star

- 1) Fe-group atoms (Ni-62, Fe-58, Fe-56) have maximum binding energy: no more energy released by fusion
→ stellar core starts collapsing because pressure drops
- 2) electron degeneracy pressure tries to stop collapse but if core mass $>$ Chandrasekhar mass ($\sim 1.4 M_{\text{sun}}$)
electron + proton capture removes electrons
→ electron pressure decreases



- COLLAPSE to NUCLEAR DENSITY,
where neutron degeneracy pressure stops collapse
- PROTO-NEUTRON STAR FORMS

Fraction of binding energy of core ($E_{b,c} \sim 10^{53}$ erg)

$$W \sim 5 \times 10^{53} \text{ erg} \left(\frac{M_{\text{PNS}}}{1.4 M_{\odot}} \right)^2 \left(\frac{10 \text{ km}}{R_{\text{PNS}}} \right)$$

used to launch a **SHOCK** := supernova explosion

MECHANISM that converts binding energy into shock is **UNKNOWN**

Convective engine?

Rotational instability?

Magnetically driven explosion?

STANDARD MODEL: CONVECTIVE ENGINE

Potential energy is converted into thermal energy
(mostly thermal energy of neutrinos)
and core bounces driving shocks

SHOCK MUST REVERSE COLLAPSE OF OUTER LAYERS

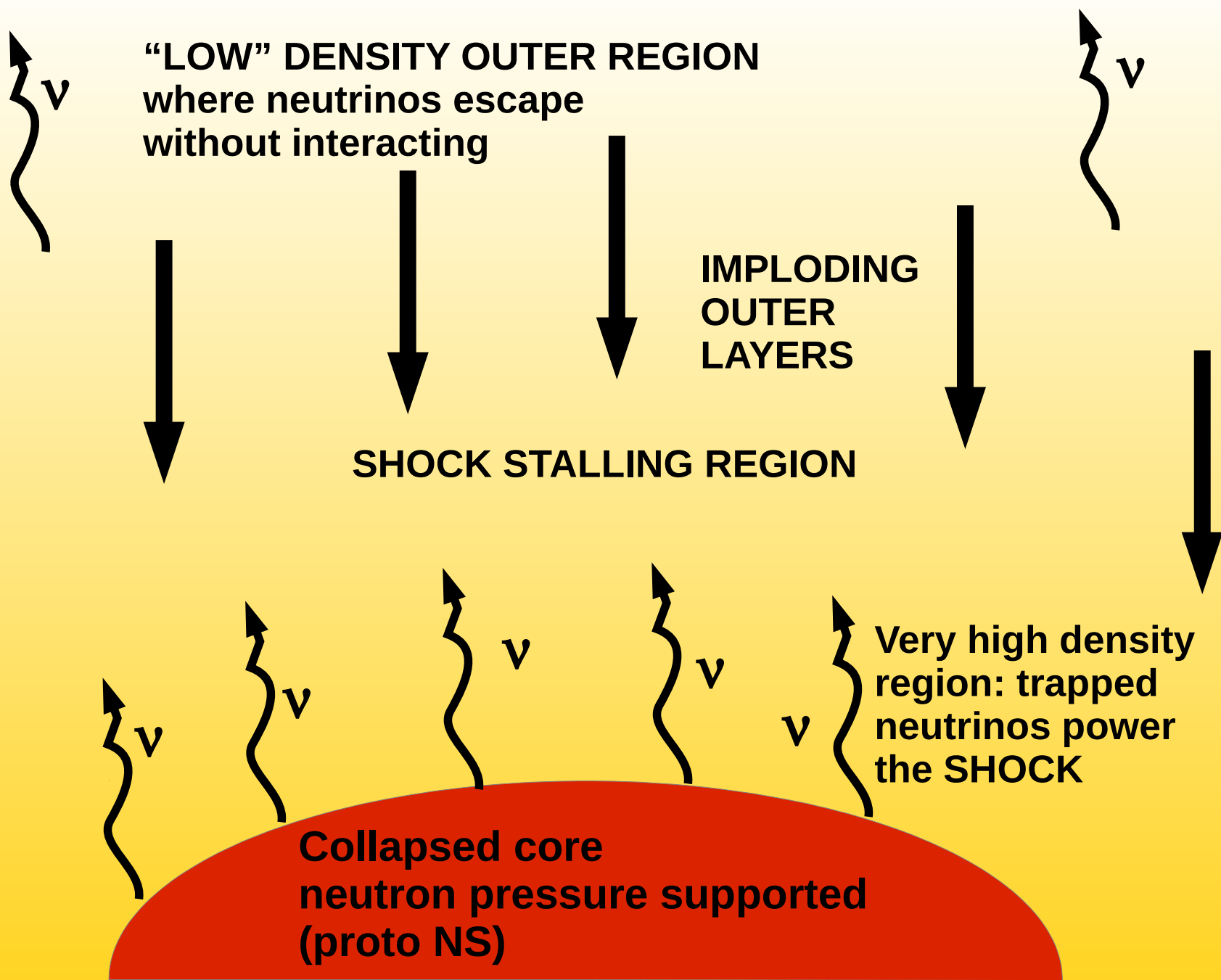
But density must be sufficiently high that neutrinos interact,
otherwise neutrinos leak away without transferring energy

- **SHOCK MIGHT STALL**
- **SN FAILS**

WHEN DOES THE SHOCK STALL and the SN FAILS?

Convective region below shock where neutrino transfer is
enhanced by convection

Fryer 2014, http://pos.sissa.it/archive/conferences/237/004/FRAPWS2014_004.pdf



How to study a core-collapse supernova (SN)?

HYDRODYNAMICAL SIMULATIONS

!!CAVEAT: only stars with mass 8 – 11 Msun explode easily!!

1D: large statistics (hundreds of models), approximate neutrino transfer (often kinetic bombs or thermal bombs to artificially induce explosion even in more massive stars)

(O'Connor & Ott 2011; Ugliano et al. 2012; Ertl et al. 2016)

2D: explode easily but might contain wrong physics

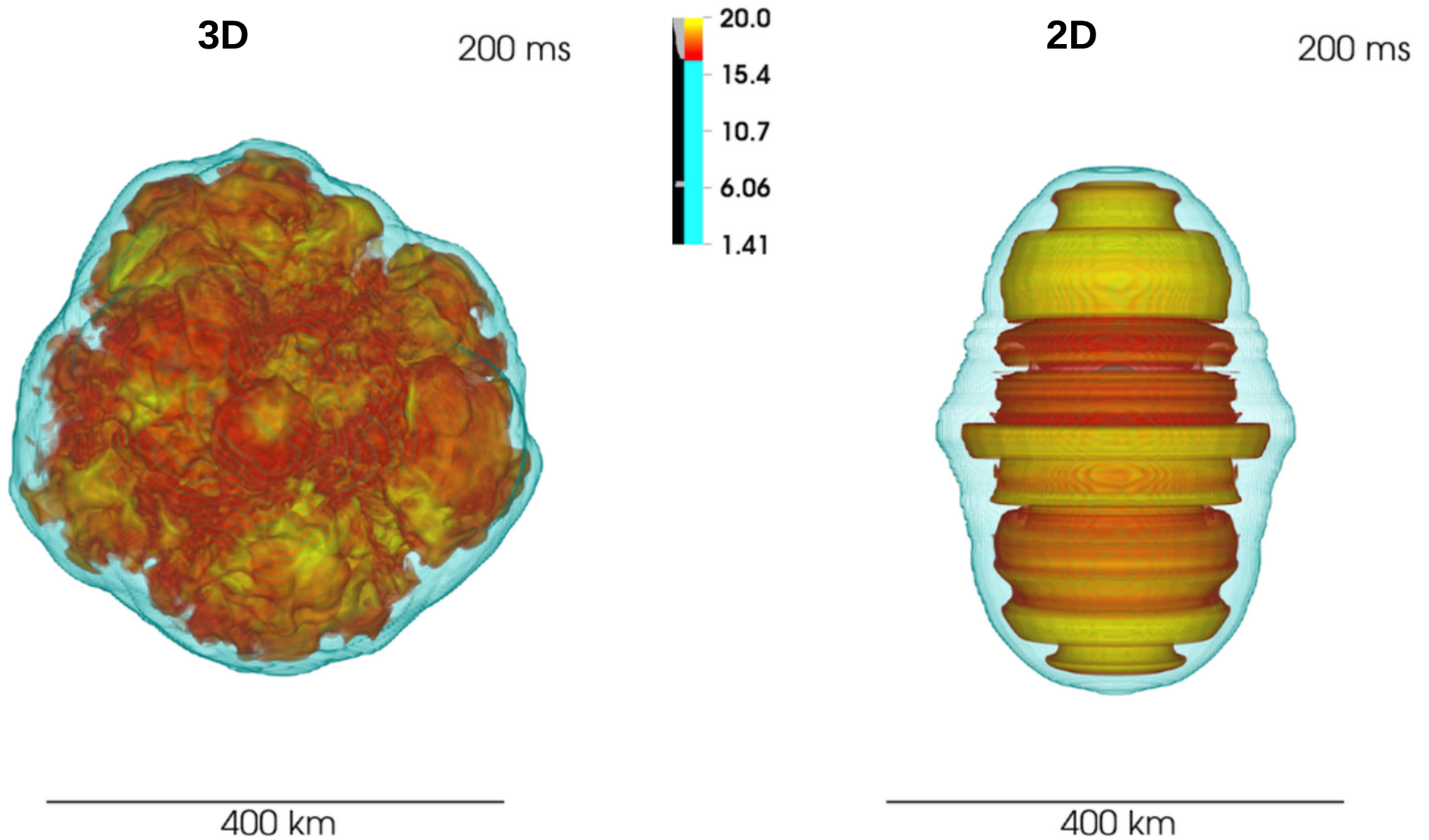
(Marek & Janka 2009; Mueller et al. 2012a, 2012b)

3D: computationally expensive, explode slowly

(Ott et al. 2005; Bondin & Mezzacappa 2007; Couch 2013; Couch & O'Connor 2014)

How to study a core-collapse supernova (SN)?

HYDRODYNAMICAL SIMULATIONS (Couch & O'Connor 2014)



Supernova shock stops if BOUND MASS is too LARGE (Fryer 1999; Fryer & Kalogera 2001)

Back-of-the-envelope calculation to connect direct collapse
and pre-supernova mass:

$$E_{\text{SN}} = \frac{G M_{\text{env}} (M_{\text{env}} + M_{\text{core}})}{R_{\text{env}}}$$

envelope mass \rightarrow proto-NS $\sim 1 M_{\text{sun}}$
 envelope radius

Star cannot explode if
envelope binding energy
> SN energy

$$M_{\text{env}} \sim 50 M_{\odot} \left(\frac{E_{\text{SN}}}{10^{51} \text{erg}} \right)^{1/2} \left(\frac{R_{\text{env}}}{10 R_{\odot}} \right)^{1/2}$$

If $M_{\text{fin}} > 50 M_{\text{sun}}$ this SN fails and star collapses to a BH!

CRITERIA FOR COLLAPSE TO A REMNANT

depends on the "compactness" of the inner layers of the star

1. MASS OF CARBON-OXYGEN CORE

If $M_{\text{co}} > 7 - 8 M_{\text{sun}}$ SN FAILS

(Fryer+ 1999, 2012; Belczynski+ 2010)

2. COMPACTNESS

3. TWO-PARAMETER CRITERION

2. COMPACTNESS (= ratio between mass and radius) of a given portion of the stellar core at the onset of collapse
(O'Connor & Ott 2011, Ugliano et al. 2012)

$$\xi_M \equiv \frac{M / M_{\odot}}{R(M) / 1000 \text{ km}}$$

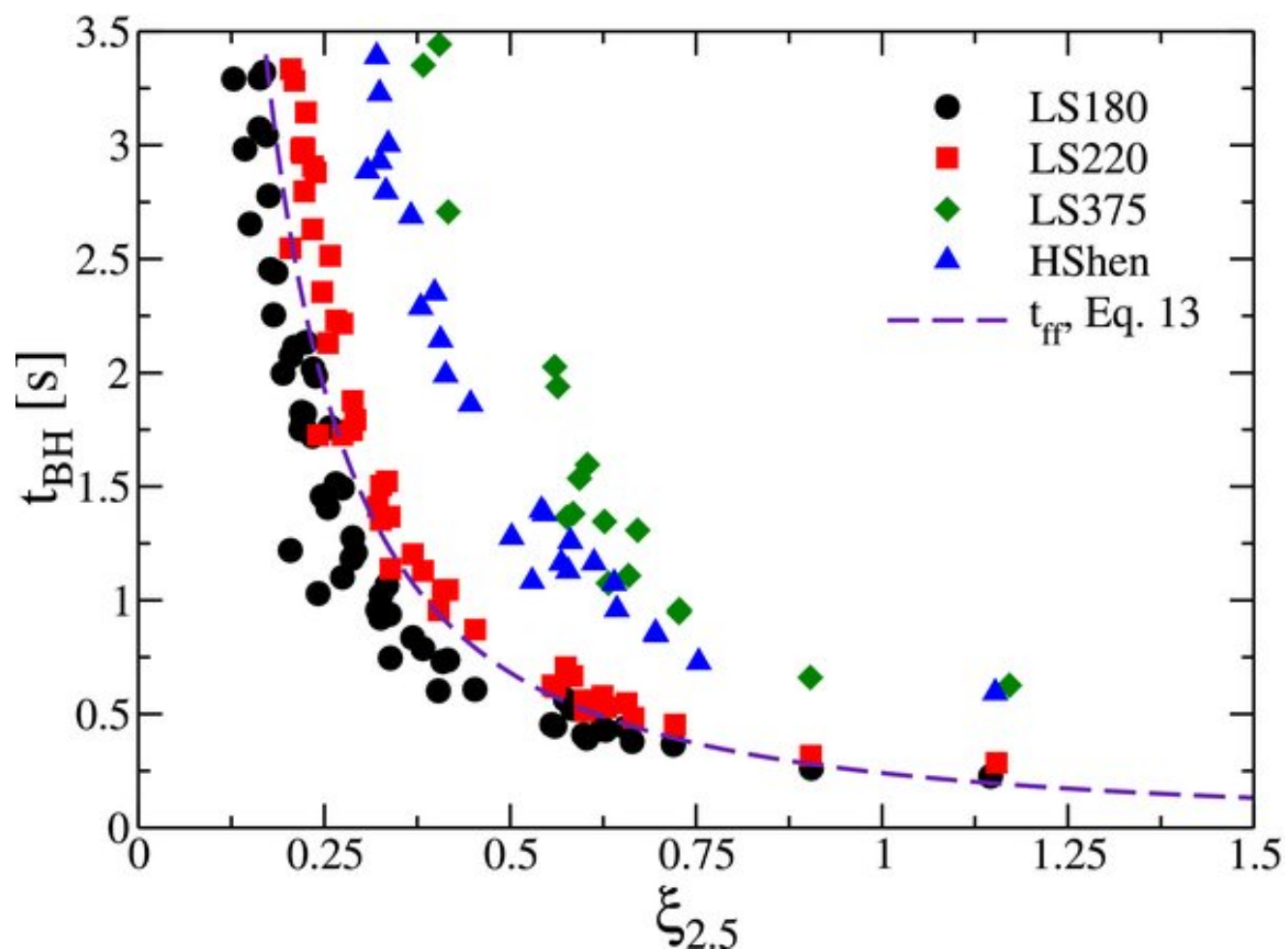
$M = 2.5 M_{\odot}$ is usually adopted

**Time for BH formation
strong function of
compactness at 2.5 Msun**

Star collapses if

$$\xi_{2.5} > 0.2$$

(Horiuchi et al. 2014)



2. COMPACTNESS

Compactness criterion and CO core criterion agree

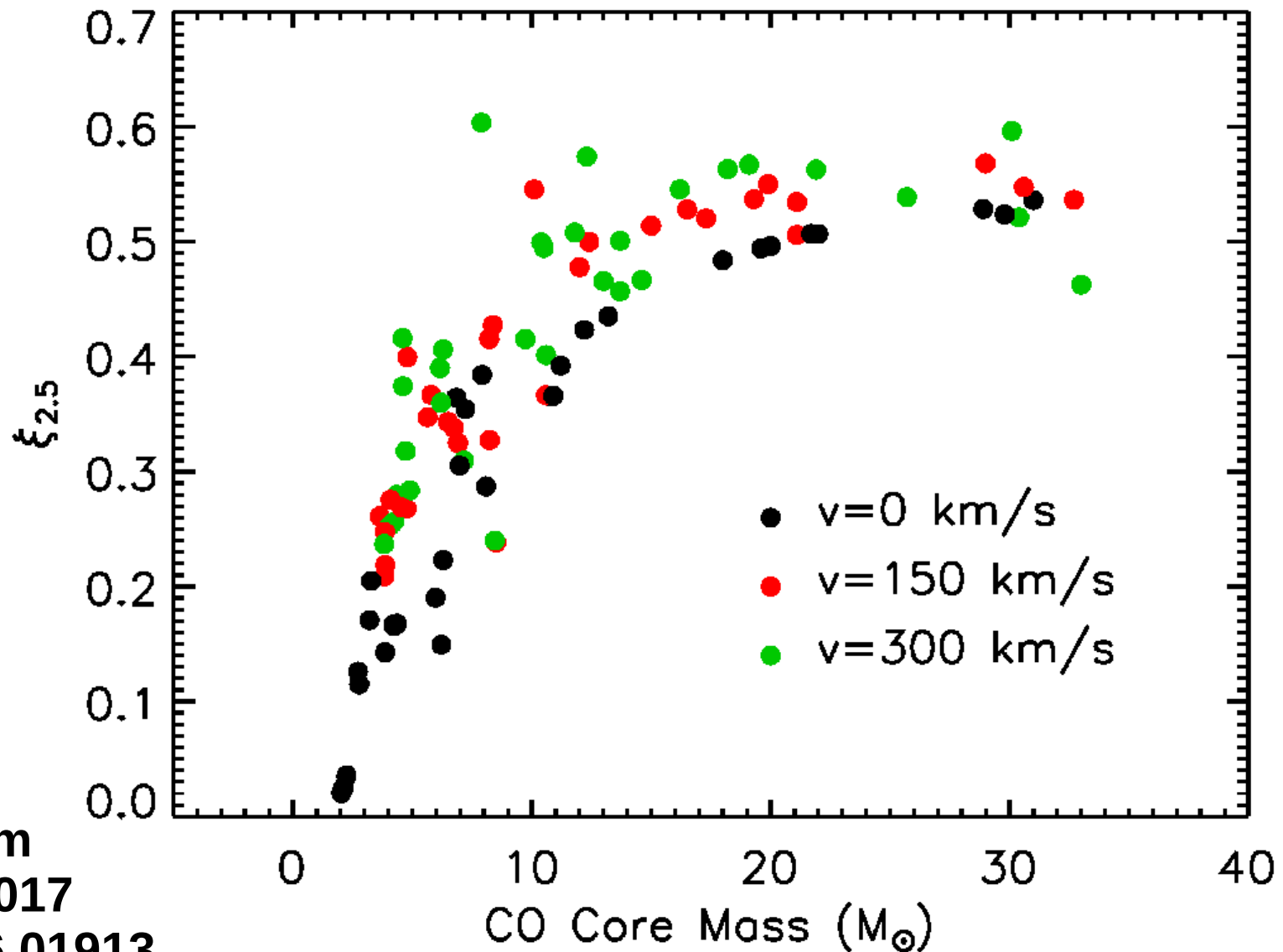
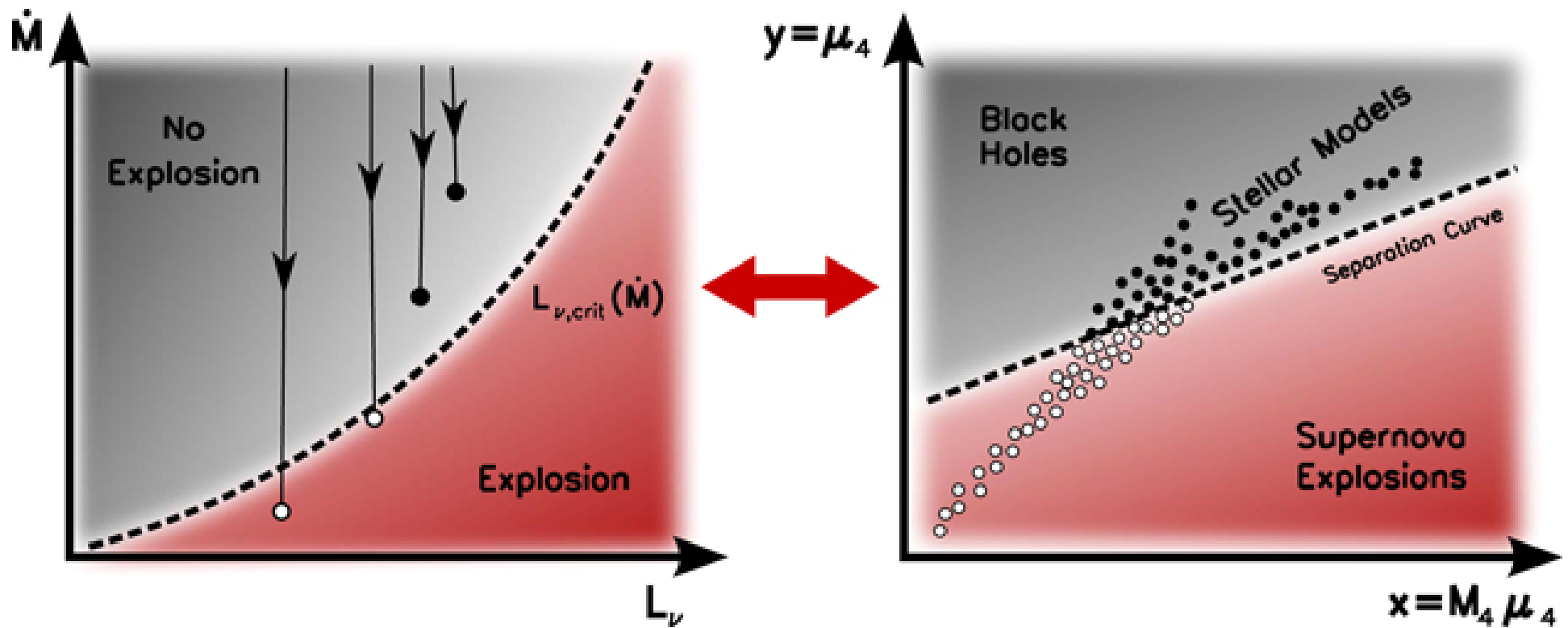


Figure from
Limongi 2017
arXiv:1706.01913

3. enclosed mass (M_4) and mass gradient (μ_4) at a dimensionless entropy per nucleon $s = 4$

$$M_4 = m(s = 4) / M_\odot$$

$$\mu_4 = \left[\frac{dm / M_\odot}{dr / 1000 \text{ km}} \right]_{s=4}$$



3. enclosed mass (M_4) and mass gradient (μ_4) at a dimensionless entropy per nucleon $s = 4$

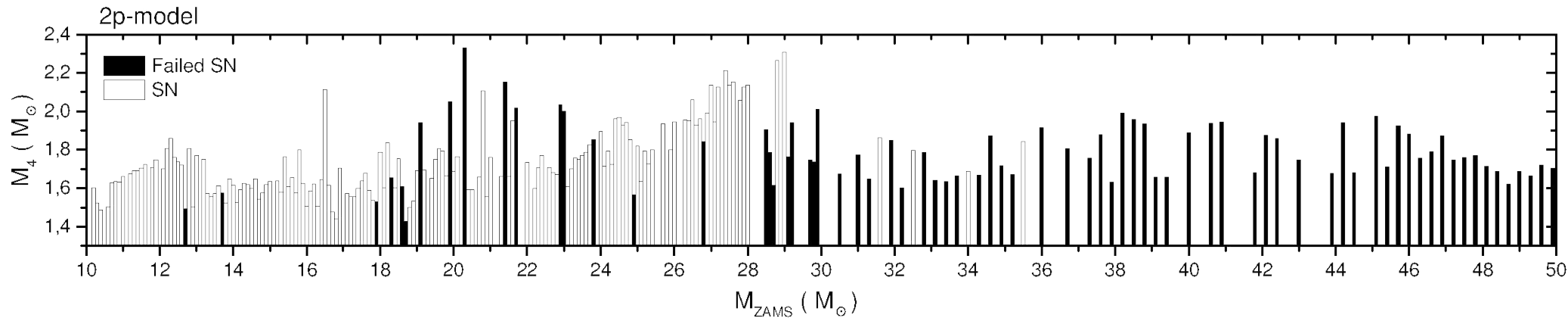


Fig. 21

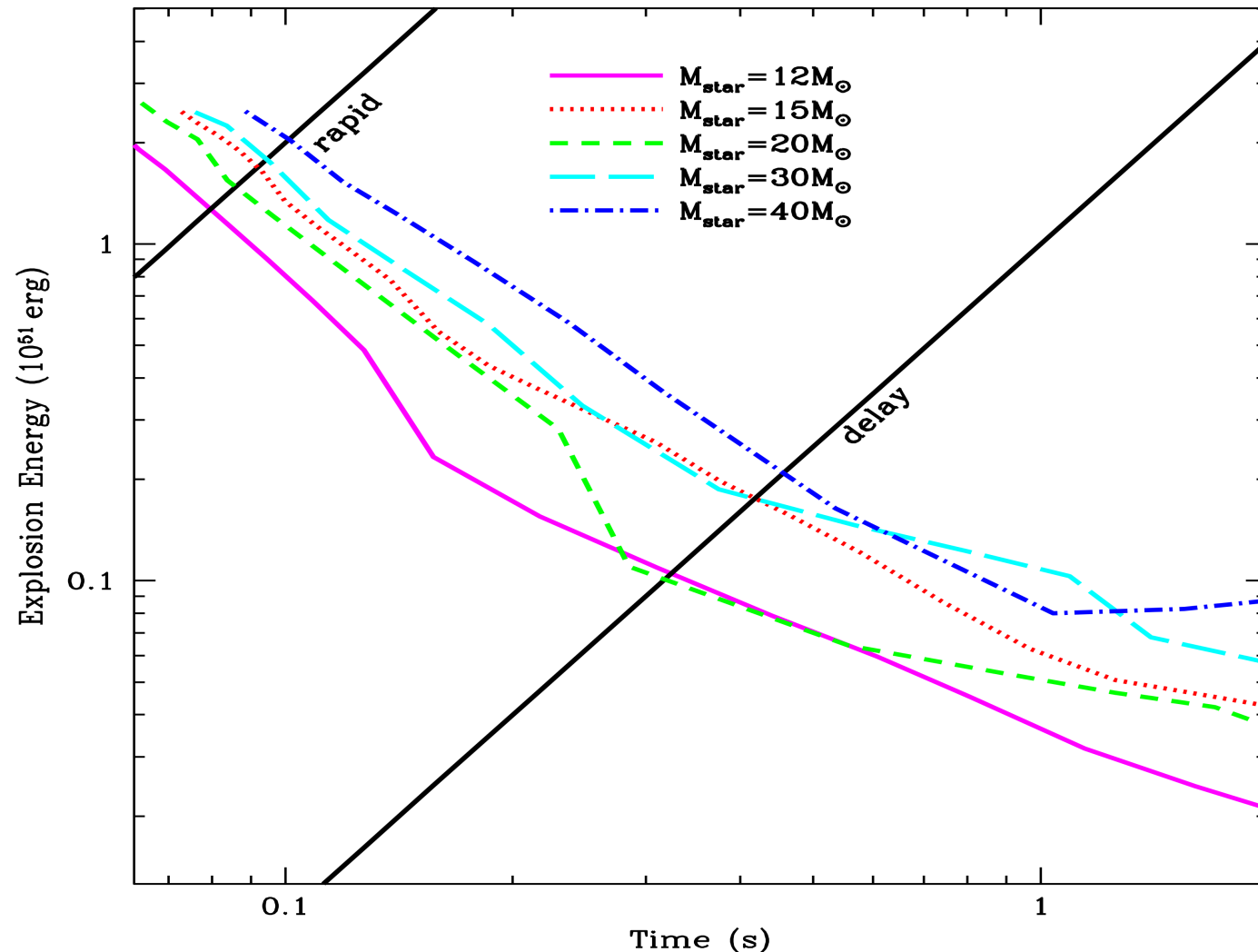
Spera, MM, Bressan 2015

ISLANDS OF DIRECT COLLAPSE AND SN EXPLOSION

Concluding remark:

**MANY MODELS of SN EXPLOSION – REMNANT MASS CONNECTION
BUT IF THE STAR IS VERY MASSIVE ($>40 M_\odot$)
THEY GIVE SIMILAR RESULT**

**SN outcome depends on the "rapidity" of the explosion
(e.g. Fryer+ 2012; Fryer 2014)**



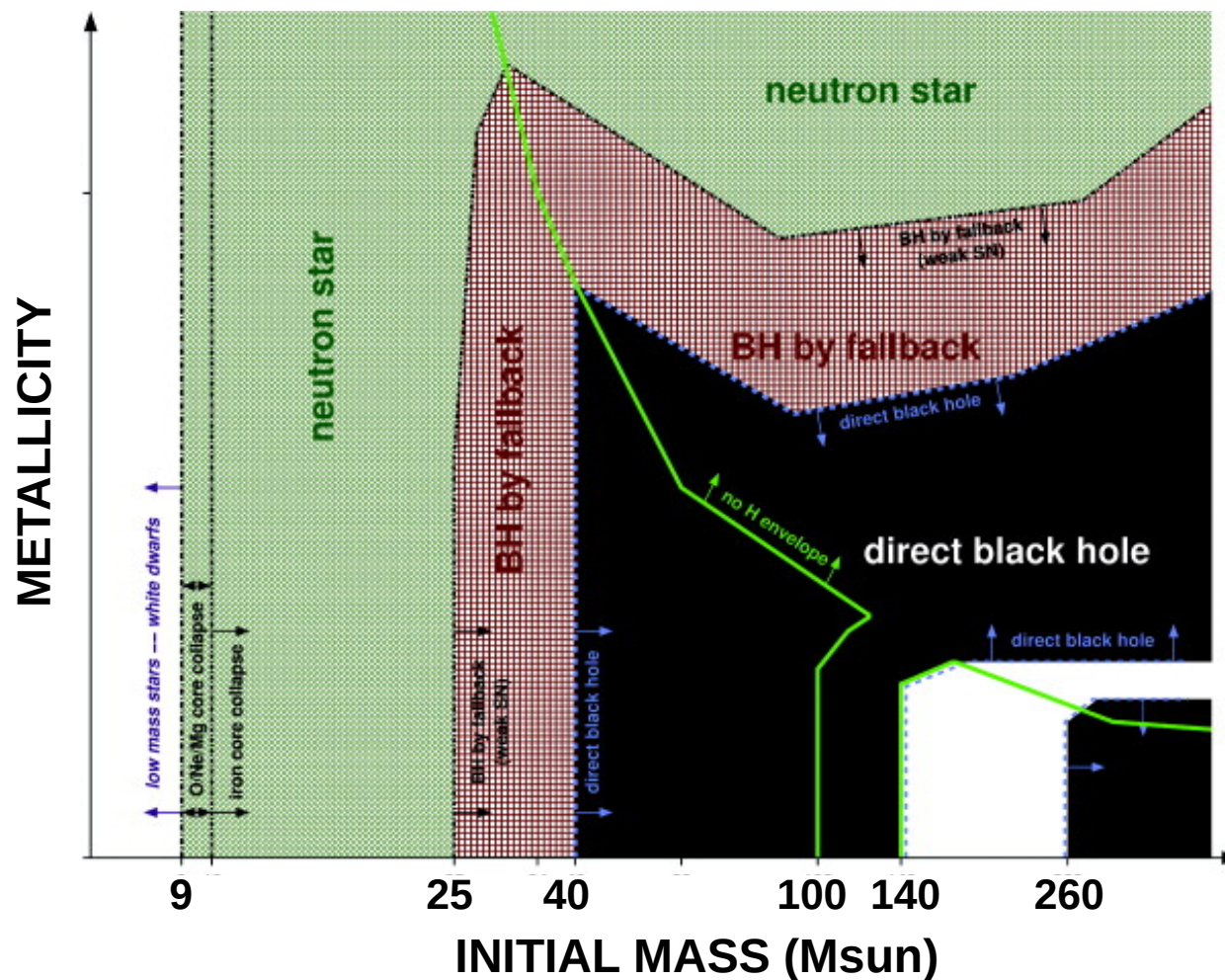
RAPID
 (<200 ms
 after bounce):
 explosion
 energy $>10^{51}$ erg/s

DELAYED
 (>200 ms
 after bounce):
 explosion
 energy $<10^{51}$ erg/s)

From Fryer 2014,

http://pos.sissa.it/archive/conferences/237/004/FRAPWS2014_004.pdf

SN outcome depends on the "fallback" of the outer layers:
How much material falls back to the proto-NS after the SN
Barely constrained – depends on explosion energy,
angular momentum,
progenitor's mass/metallicity



Heger 2003

PAIR-INSTABILITY SUPERNOVAE

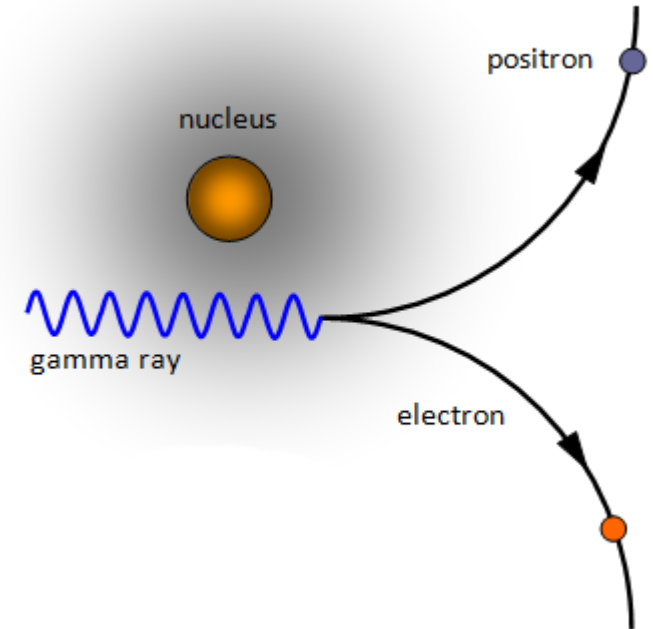
If star is very massive
(=produces γ -ray radiation in core)
 γ -ray photons scattering atomic nuclei
produce electron-positron pairs (1 Mev)

The missing pressure of γ -ray photons
produces dramatic collapse
during O burning, without Fe core

→ high-Temperature collapse ignites all remaining species

→ **an explosion is induced that leaves NO remnant**

!! Strongly depends on progenitor mass/metallicity and neutrino physics (eg Belczynski+ 2016)



PAIR-INSTABILITY SUPERNOVAE

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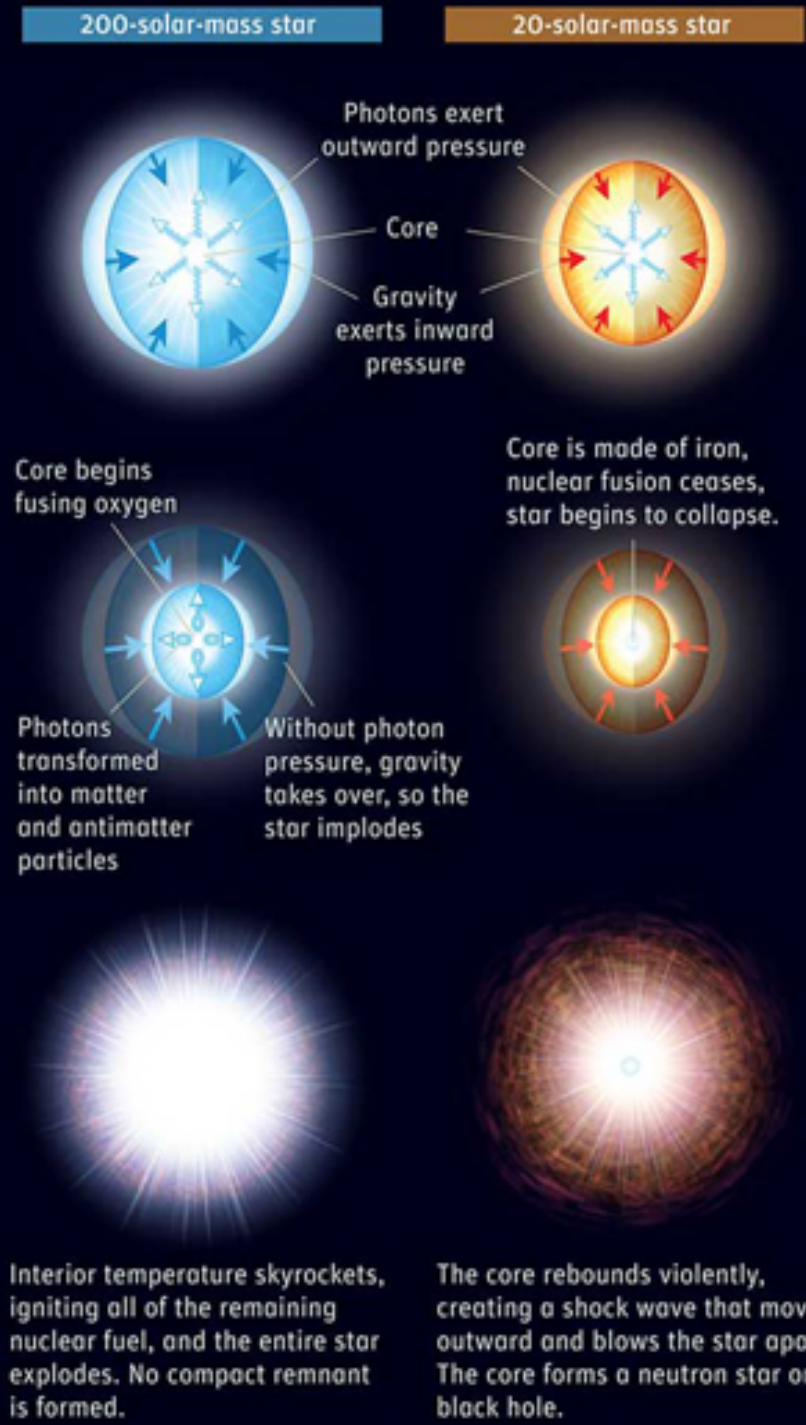
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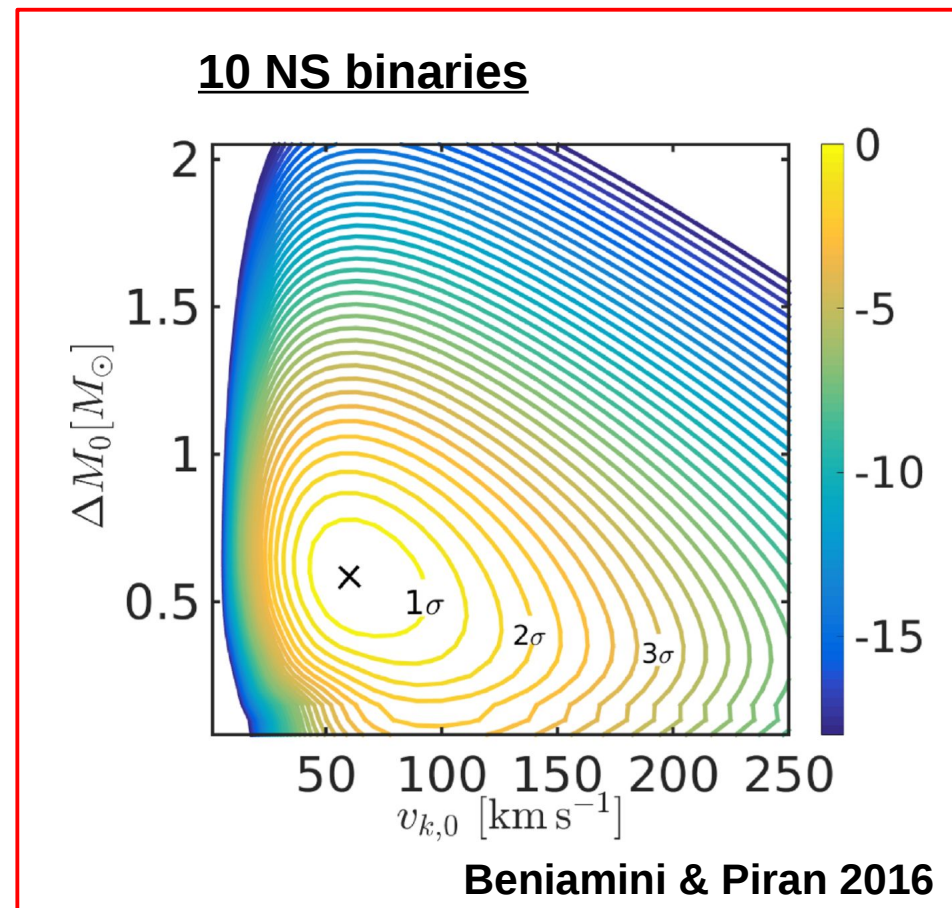
Pair-Instability Supernova vs. Core-Collapse (Type II) Supernova



ELECTRON-CAPTURE SUPERNOVAE

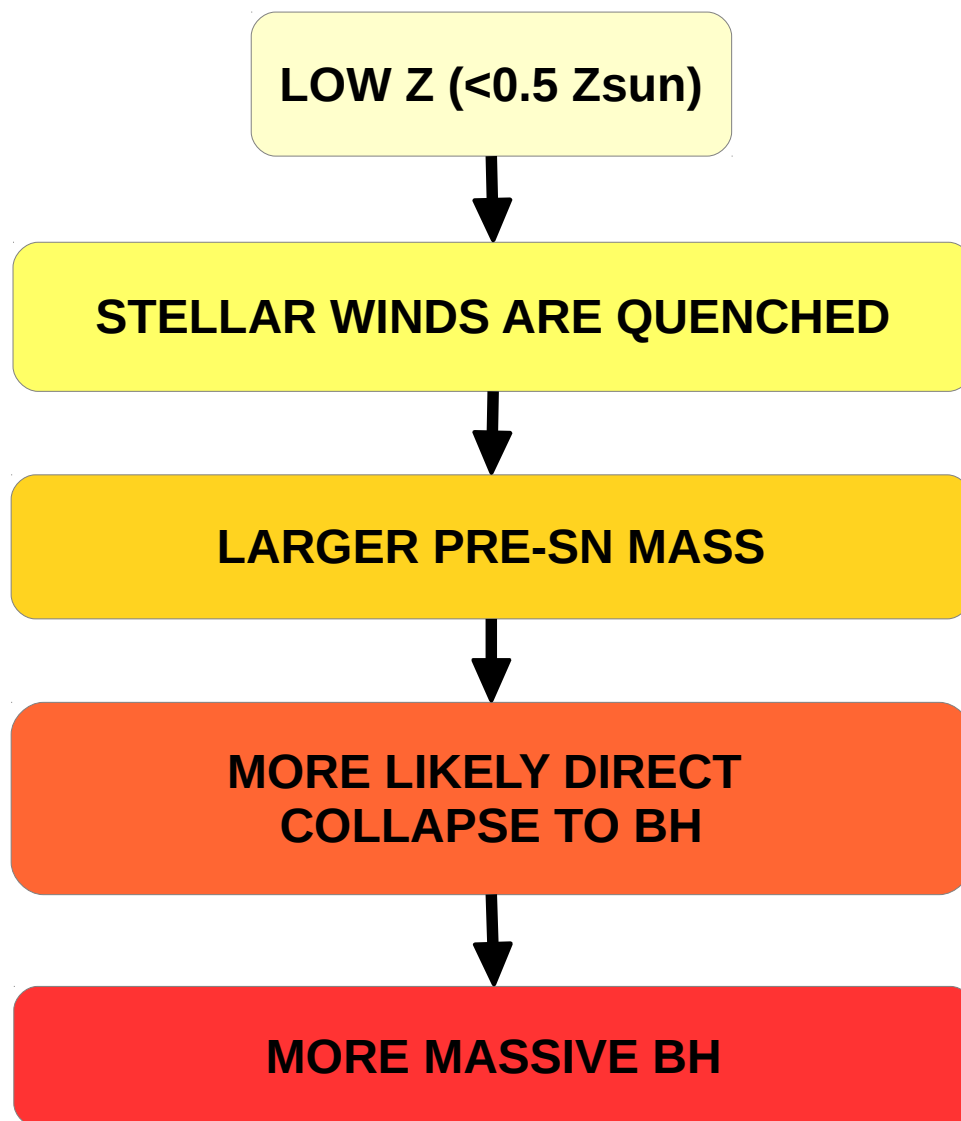
Collapse of ONe core triggered by electron capture in 5 – 10 Msun stars

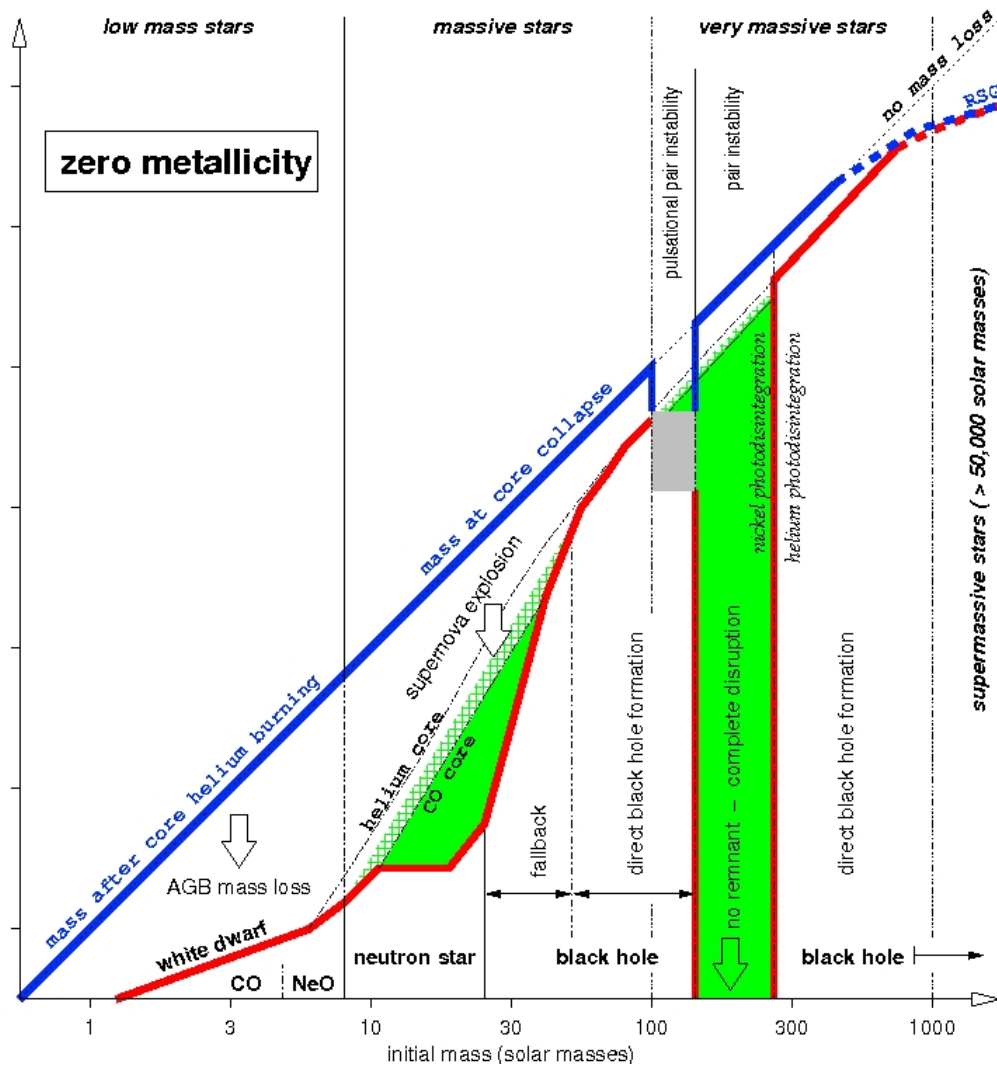
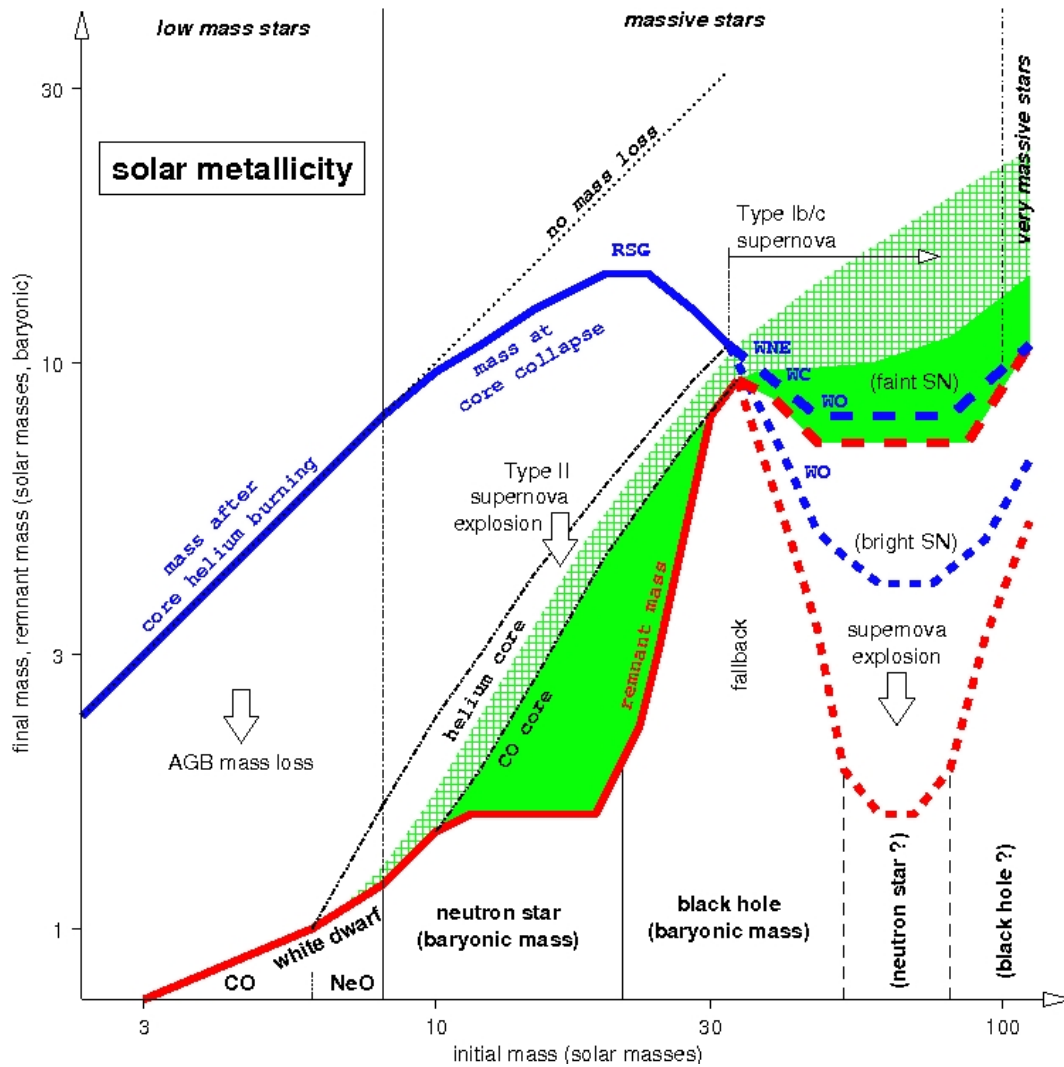
- * stars which should produce white dwarfs
- * if > 1.4 Msun ONe core is developed, electron capture is efficient onto Mg and Ne
- * removes pressure leading to core collapse (Nomoto 1984; Jones+ 2016)
- * thought to happen mostly in binaries
- * smaller NS masses (~ 1.2 Msun)
- * lower kicks (van den Heuvel 2007; Beniamini & Piran 2016)

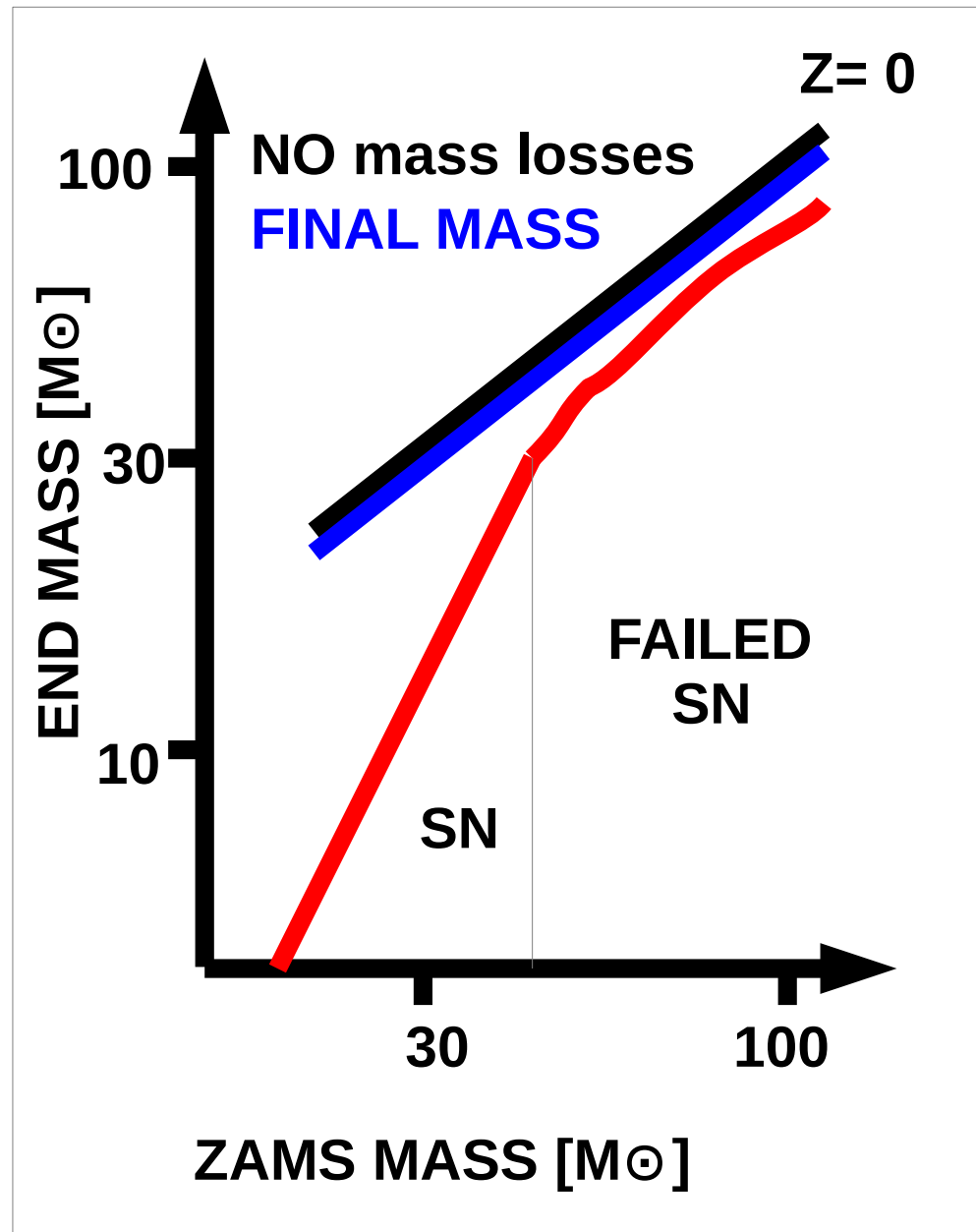
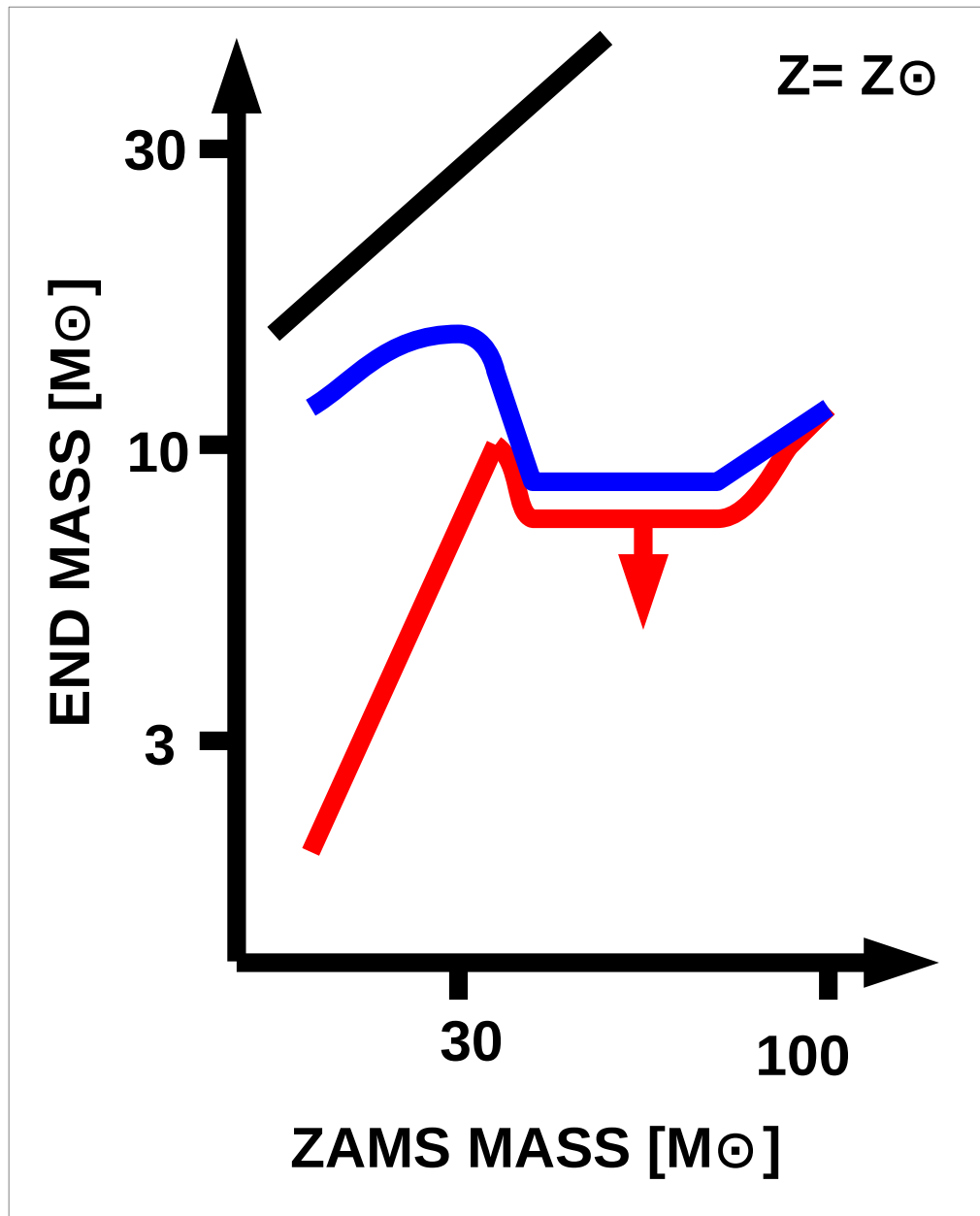


The formation of compact remnants: wrap up

Very complicated. However, as rule of thumb (MM+ 2009, 2013):







My cartoon from Heger et al. (2003)

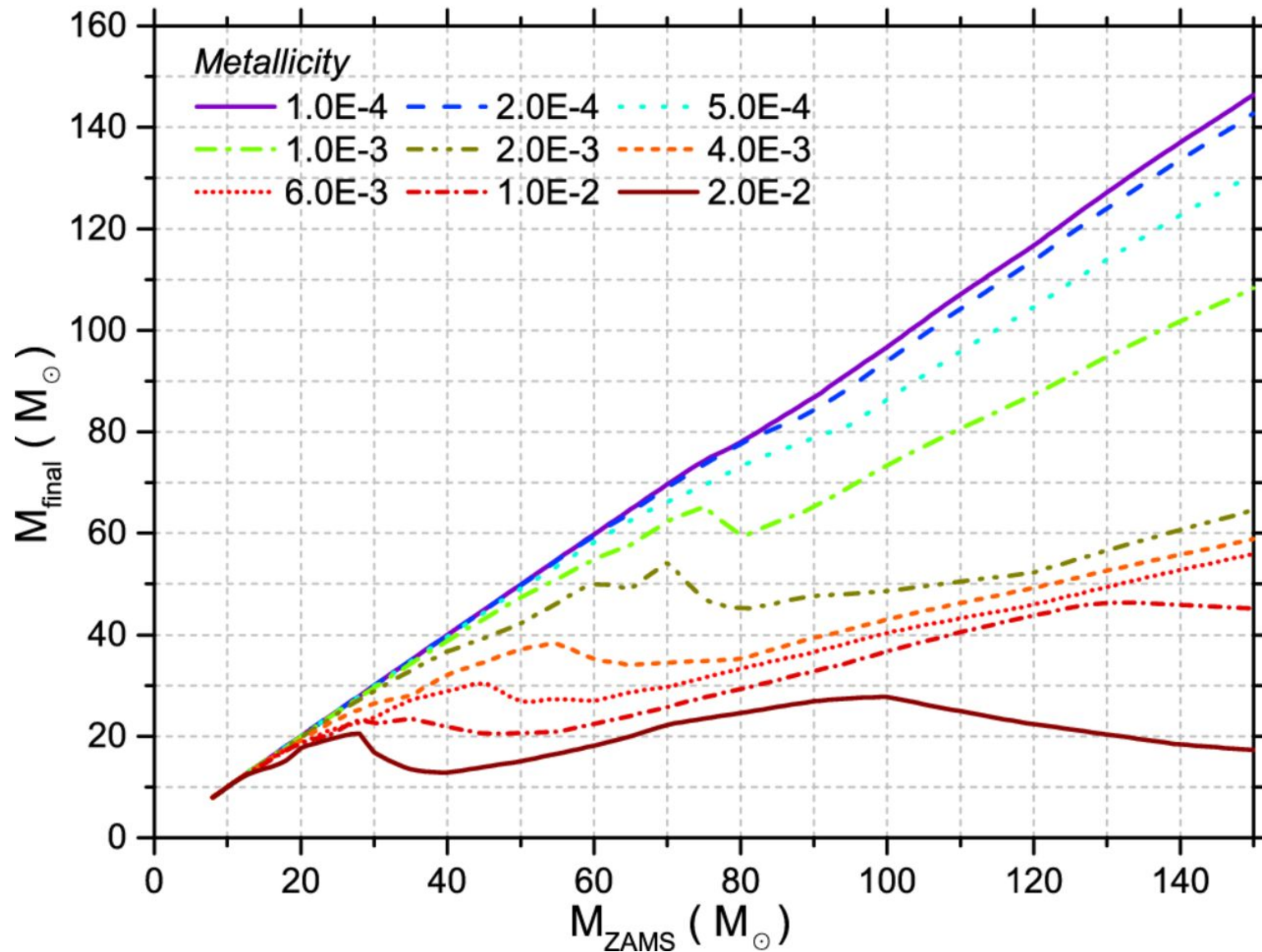
What about intermediate metallicities between 0 and solar?

- more difficult because stellar winds are uncertain

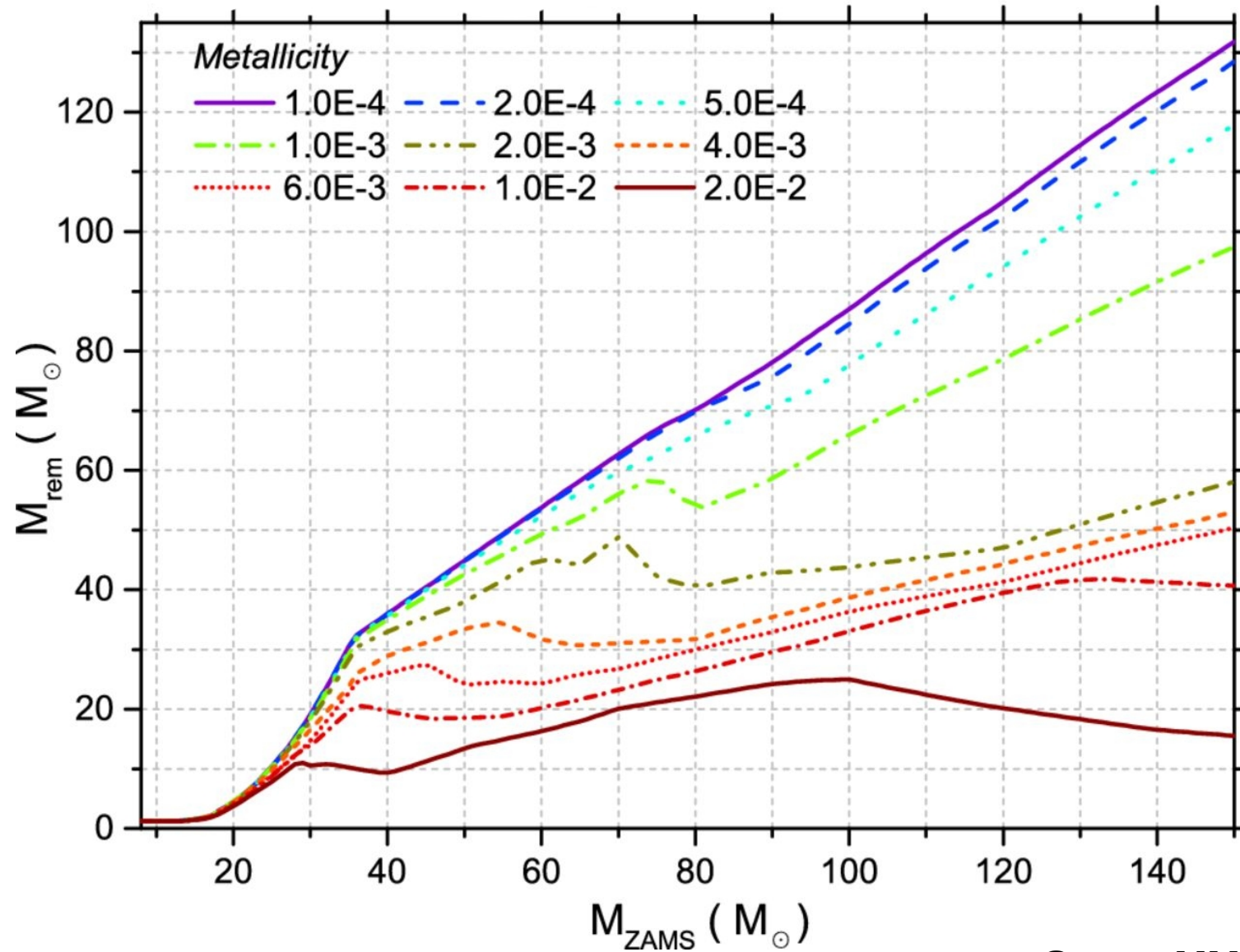
Remnant Model	Stellar Evolution	Supernova Model	Max. BH mass at $Z \sim 0.01 Z_{\text{sun}}$
MM+ 2009	Maeder+ 1992	Fryer+ 1999	~50 Msun
MM+ 2010	Portinari+ 1998	Fryer+ 1999	~80 Msun
Belczynski+ 2010	Hurley+ 2000 and Vink+ 2001	Fryer+ 1999	~80 Msun
Fryer+ 2012	Hurley+ 2000 and Vink+ 2001	Fryer+ 2012	~80 Msun
MM+ 2013,2014	SeBa (Portegies Zwart+ 2001) and Vink+ 2001		~85 Msun
Spera, MM & Bressan 2015; Spera, Giacobbo & MM 2016	PARSEC (Bressan+ 2012; Tang, Bressan+ 2014; Chen, Bressan+ 2015)	O'Connor+2011 Fryer+ 2012 Ertl+ 2015 (6 different SN models compared)	~130 Msun

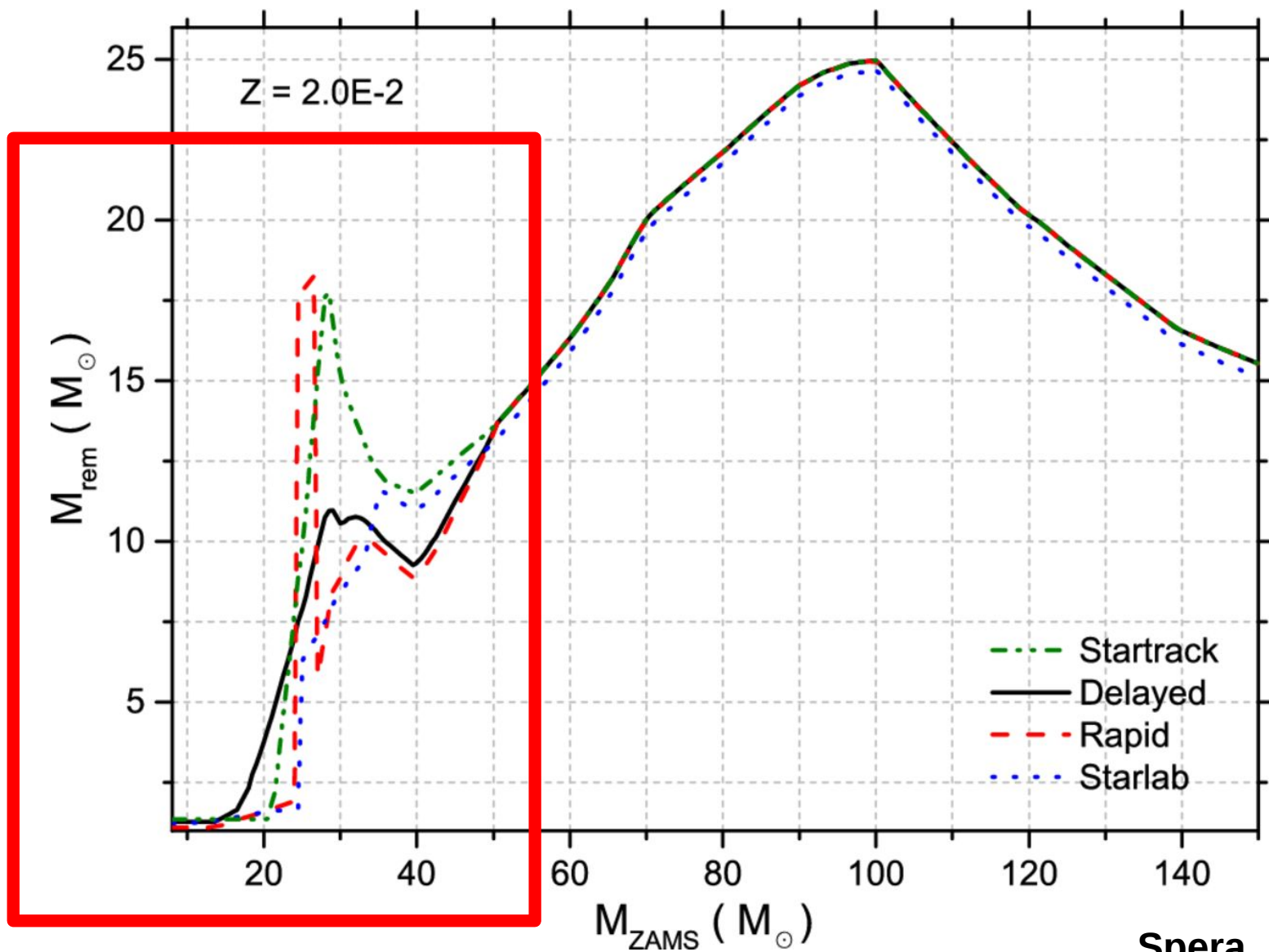
What about intermediate metallicities between 0 and solar?

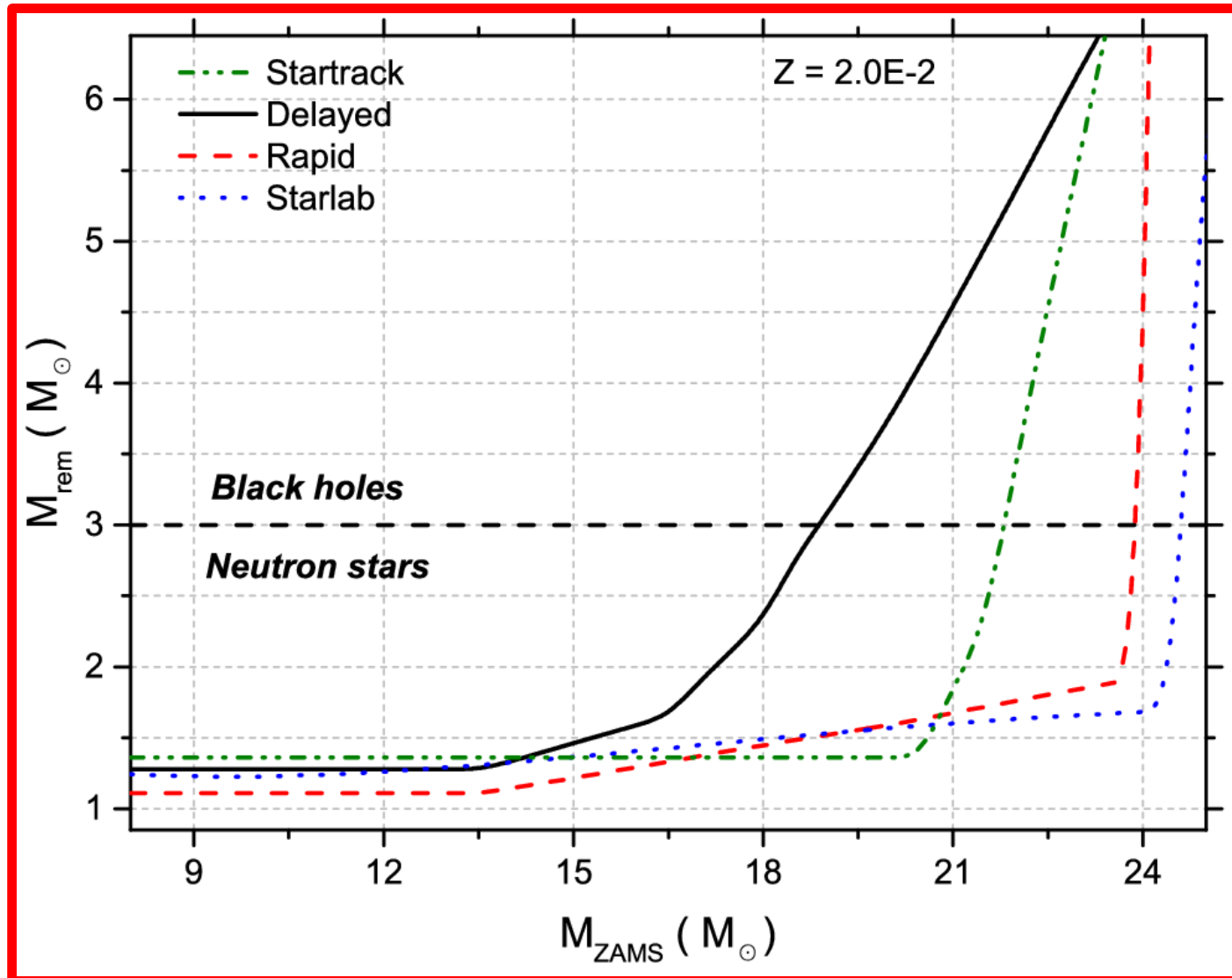
- more difficult because stellar winds are uncertain
- importance of final mass: pre-supernova mass of the star (when CO core built)



Remnant mass follows same trend as final mass
→ stellar winds are crucial



Importance of supernova model for “LOW” STAR MASSES ($<40 M_{\odot}$)

Importance of supernova model for “LOW” STAR MASSES ($<40 M_{\odot}$)

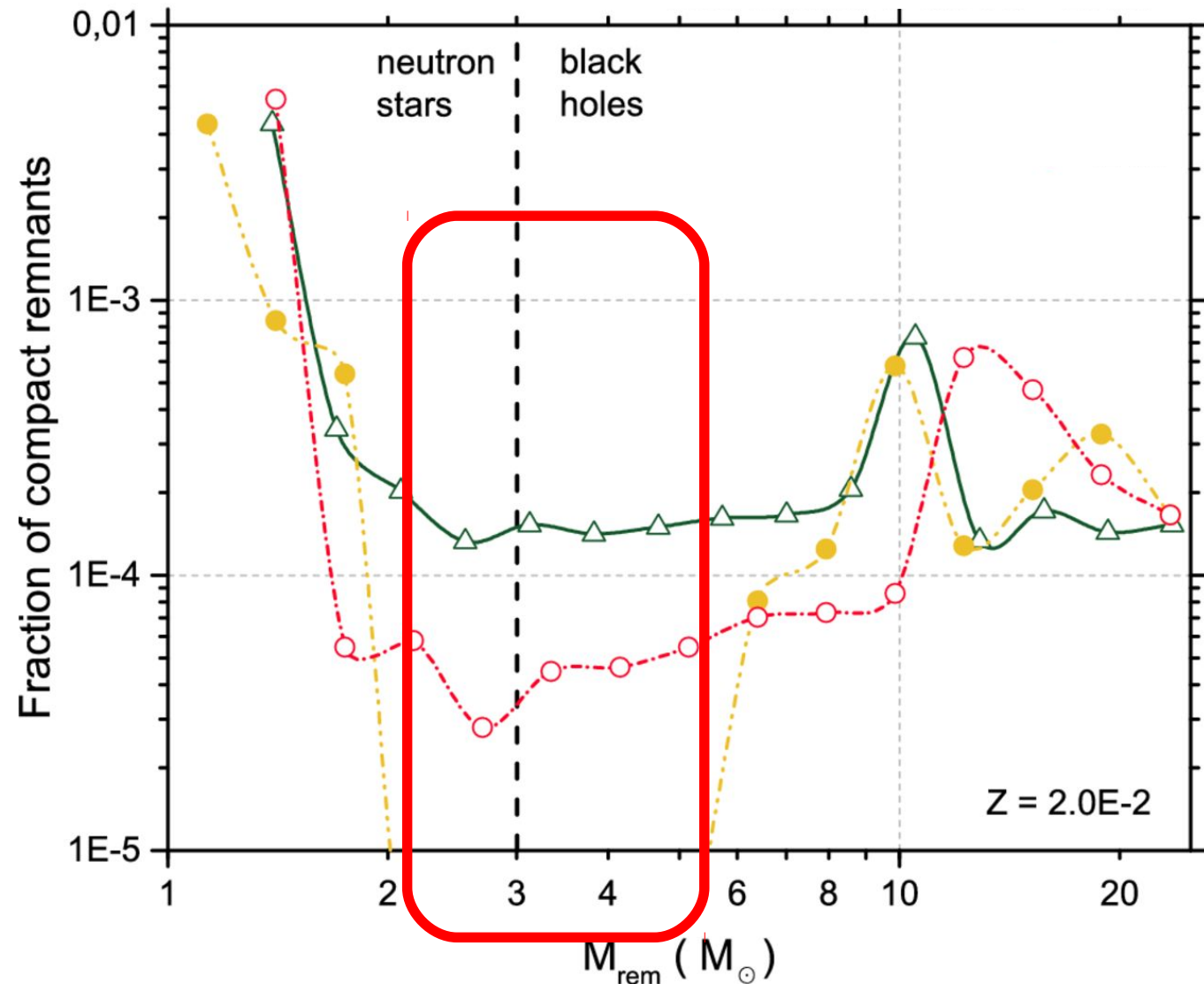
Importance of supernova model for LOW STAR MASSES (<40 M_{\odot})

Solar metallicity

GREEN:
DELAYED
SN (Fryer+ 2012)

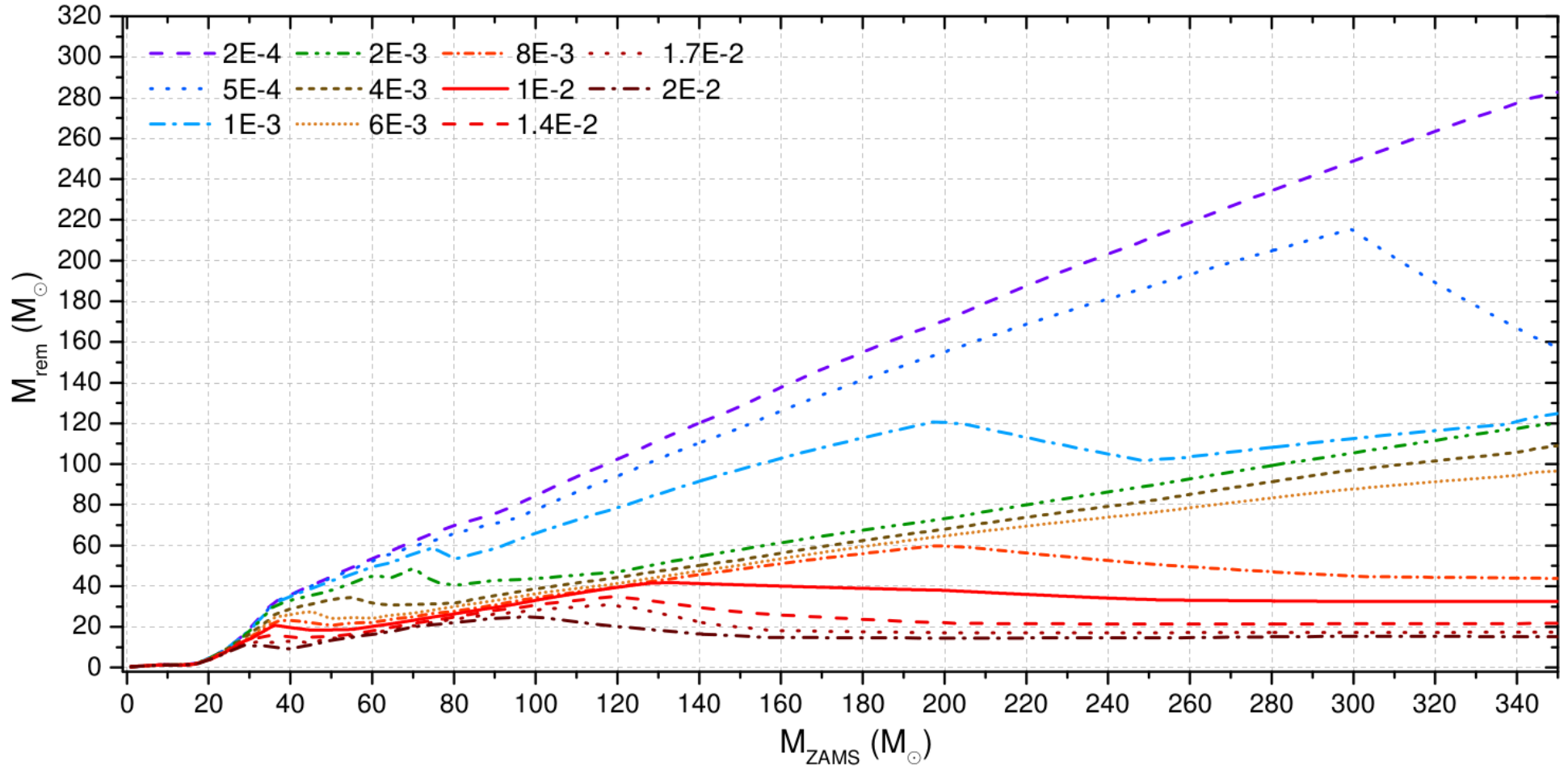
RED:
DELAYED
SN (MM+ 2013)

YELLOW:
PROMPT SN
(Fryer+ 2012)

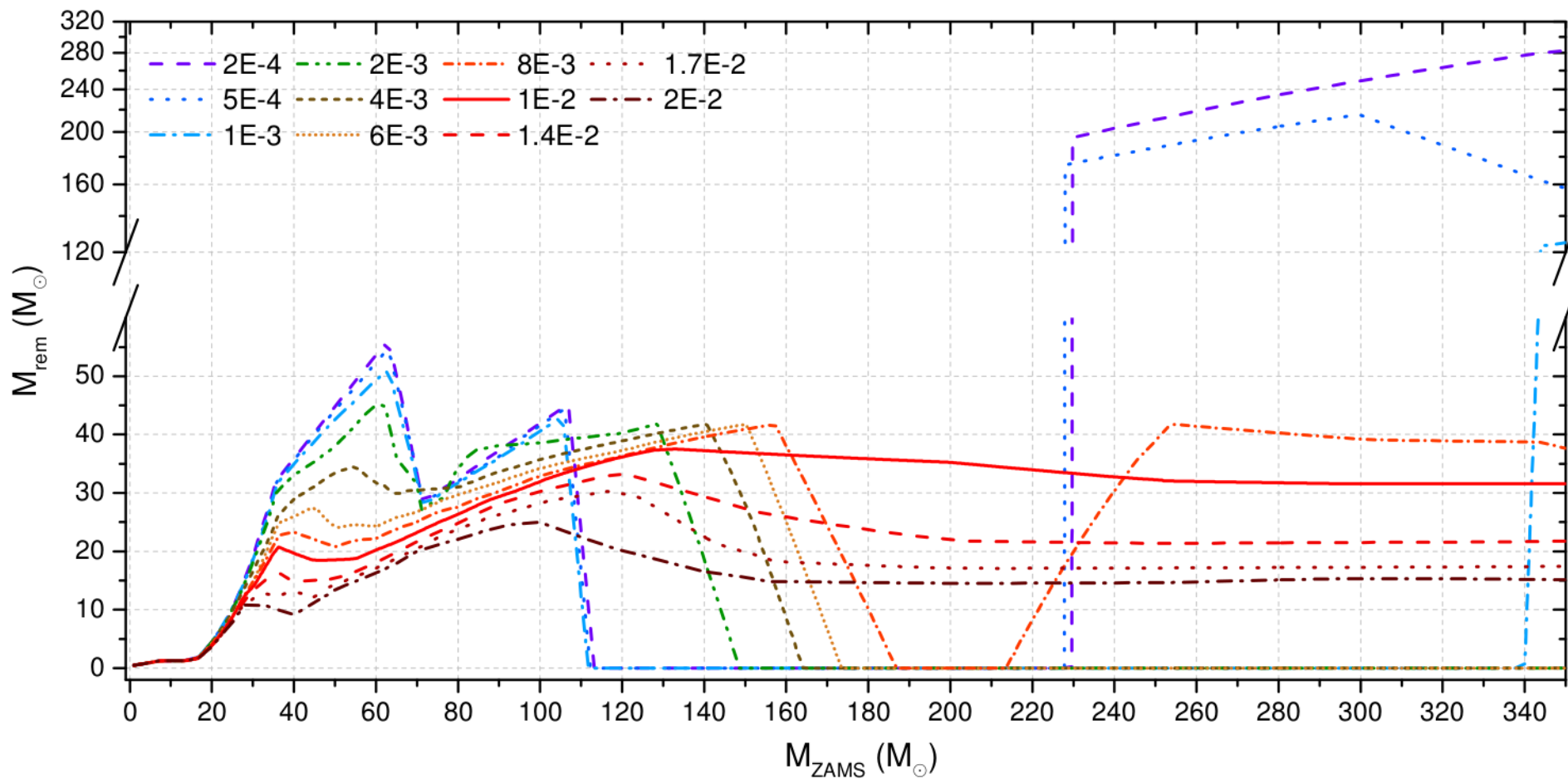


Evolution of very massive stars still uncertain

→ stellar winds are Eddington-limited rather than metallicity dependent



Role of pulsational pair-instability and pair-instability supernovae (still missing in most models)



Supernova kicks and compact-object binaries:

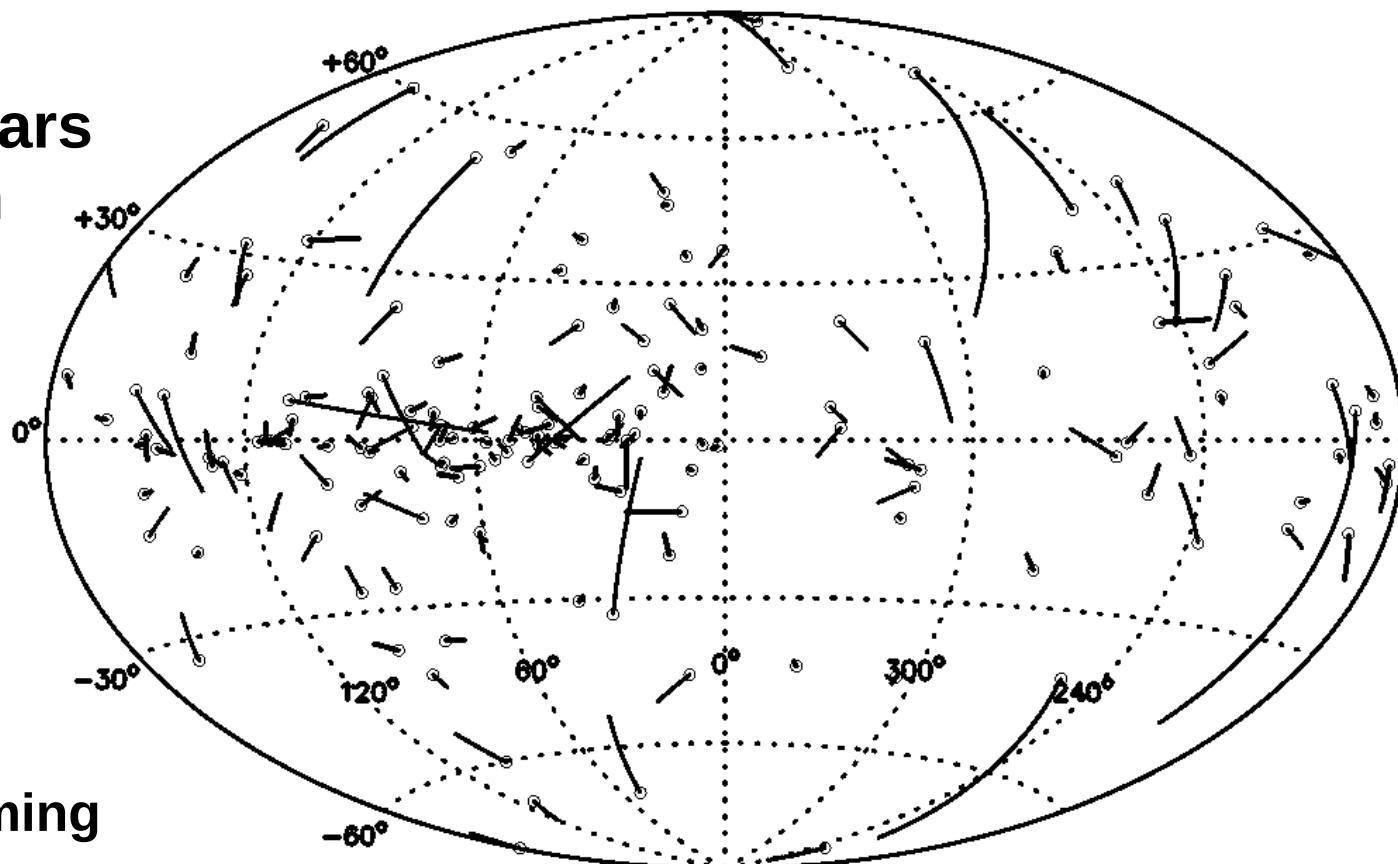
A massive-star binary can become a compact-object binary only if it is not unbound by SN kicks

SN kicks for NSs constrained from velocity of PULSARS

Hobbs+ (2005):
sample of 233 pulsars
with proper motion
measurements

A pulsar is currently
at the position
indicated by a circle

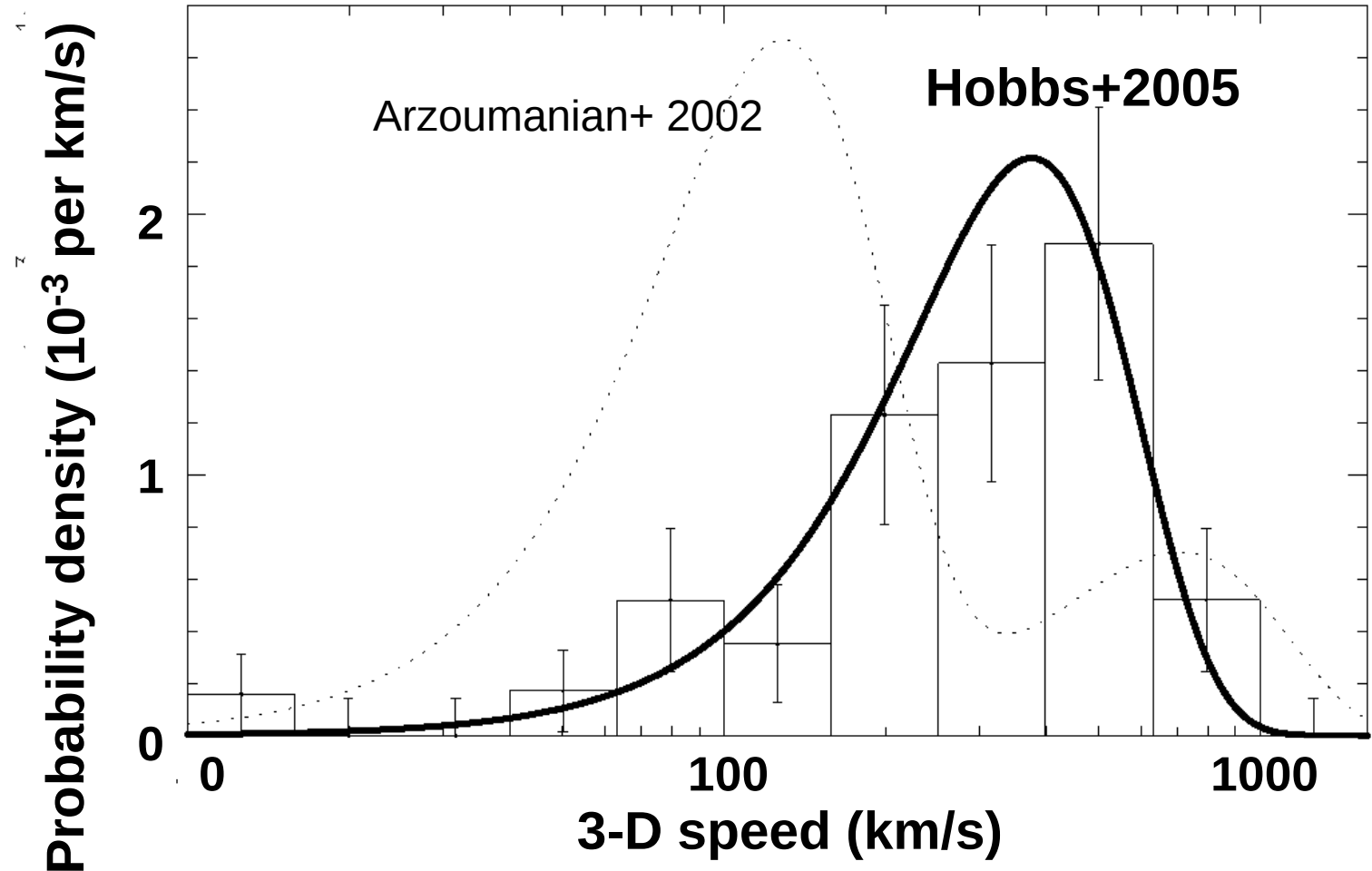
The track is its motion
for the last 1 Myr assuming
no radial velocity.



Supernova kicks and compact-object binaries:

Hobbs+ (2005): 3-D velocity distribution of pulsars obtained from the observed 2-D distributions of pulsars

→ Maxwellian distribution with $\sigma \sim 265$ km/s



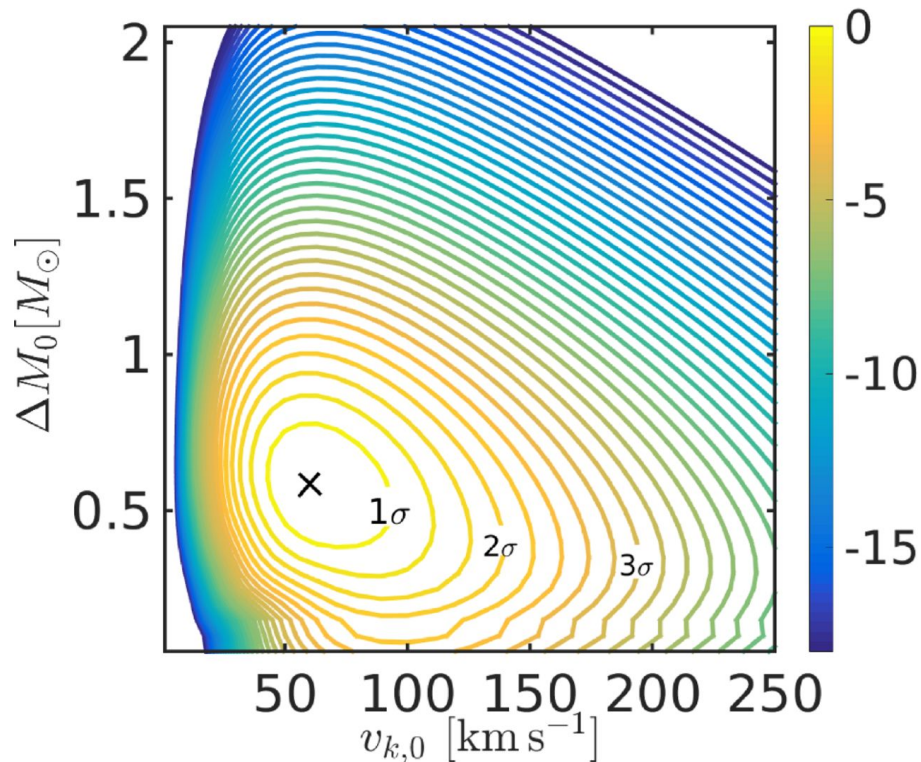
Supernova kicks and compact-object binaries:

Beniamini & Piran 2016:

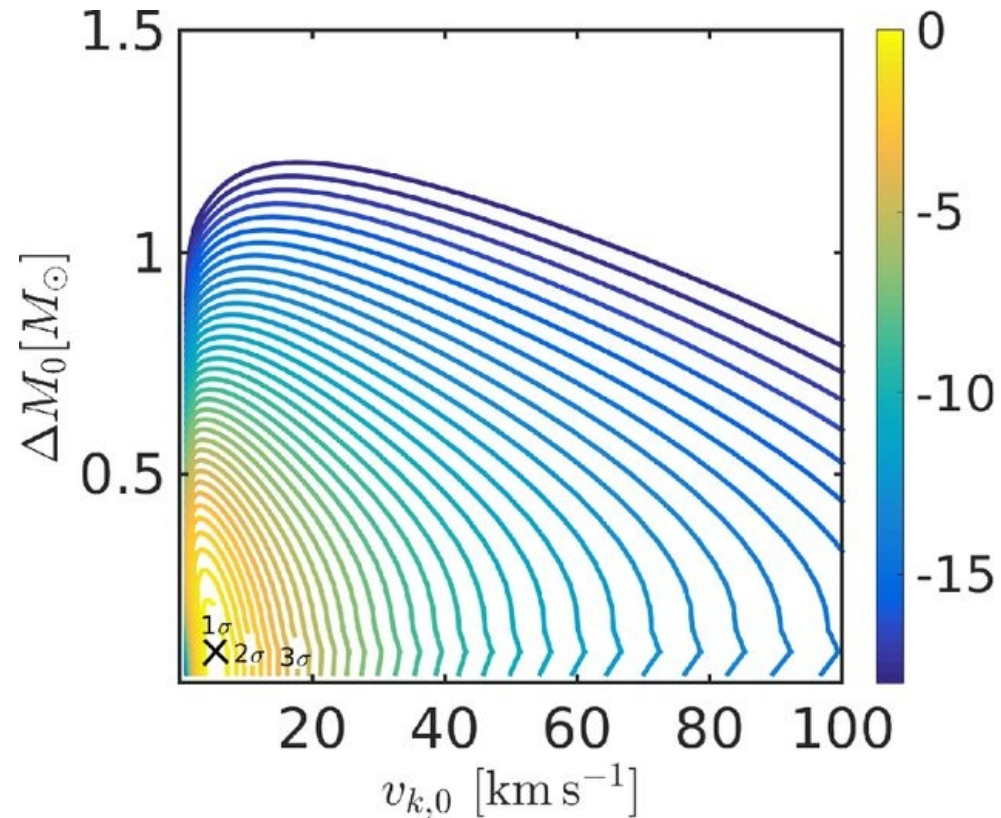
Estimate kick of double neutron stars only

Maximum likely-hood of ejected mass and kick
from conservation of energy and angular momentum

10 NS binaries



6 NS binaries with small eccentricity



Supernova kicks and black hole binaries:

WHAT ABOUT black holes?

No reliable methods to measure. Then people assume

1. conservation of linear momentum

$$v_{\text{kick, BH}} = \frac{m_{\text{NS}}}{m_{\text{BH}}} v_{\text{kick, NS}}$$

**2. BHs formed without SN (failed or direct collapse)
get NO KICK + kick modulated by FALLBACK**

$$v_{\text{kick, BH}} = (1 - f_{\text{fb}}) v_{\text{kick, NS}}$$

THANK YOU